

Holography and Quantum Error Correction

Part I:

**Non-Euclidean Geometry and
Black Holes**

اصول موضوع هندسه اقلیدسی

یک- بین هر دو نقطه می توان یک خط راست کشید،

دو- هر خطی بین دو نقطه را می توان به میزان دلخواه امتداد داد،

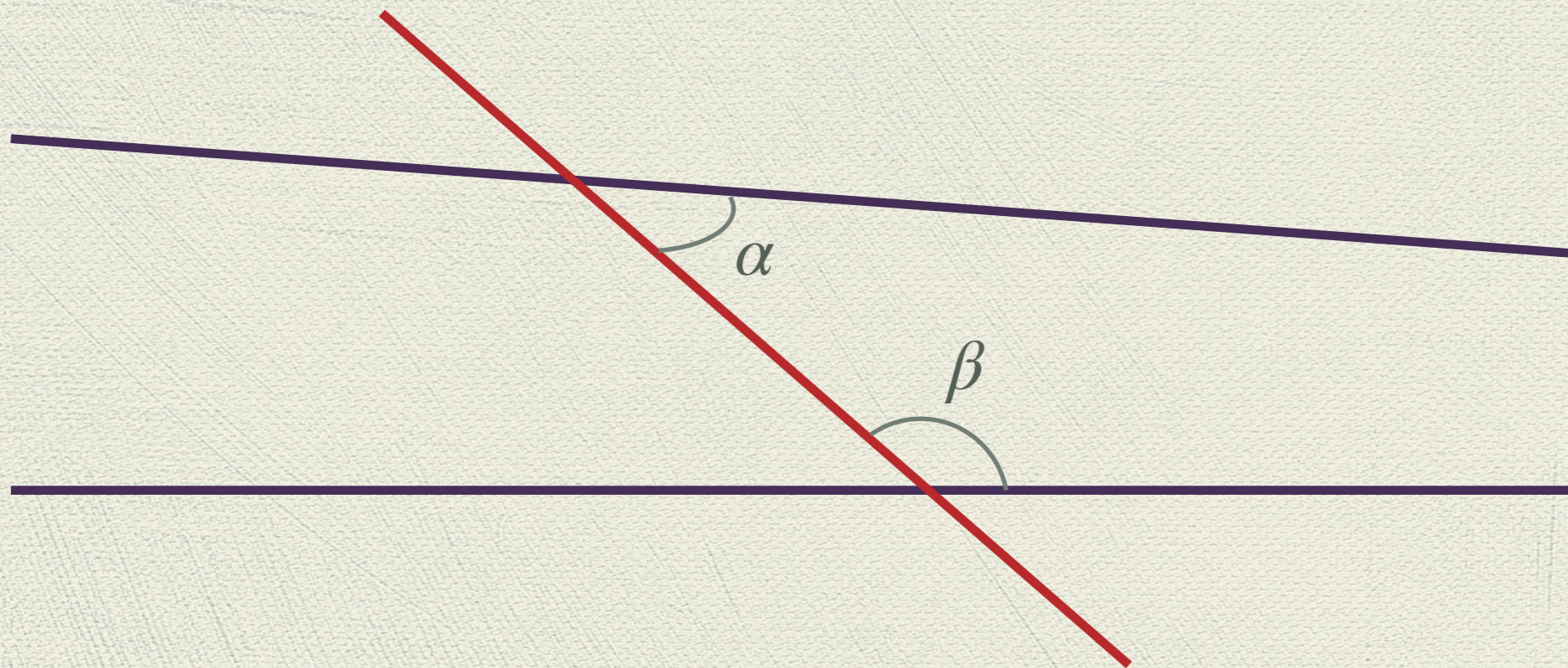
سه - می توان هر دایره ای با هر مرکزی و هر شعاعی رسم کرد،

چهار - تمام زوایای قائمه با هم مساوی هستند،

پنج - اگر خط راستی دو خط راست دیگر را قطع کند، و مجموع زوایای ایجاد شده در یک طرف از دو قائمه کمتر باشد، آن دو خط نهایتاً در آن طرف به هم خواهند رسید.

The fifth postulate

The parallel postulate

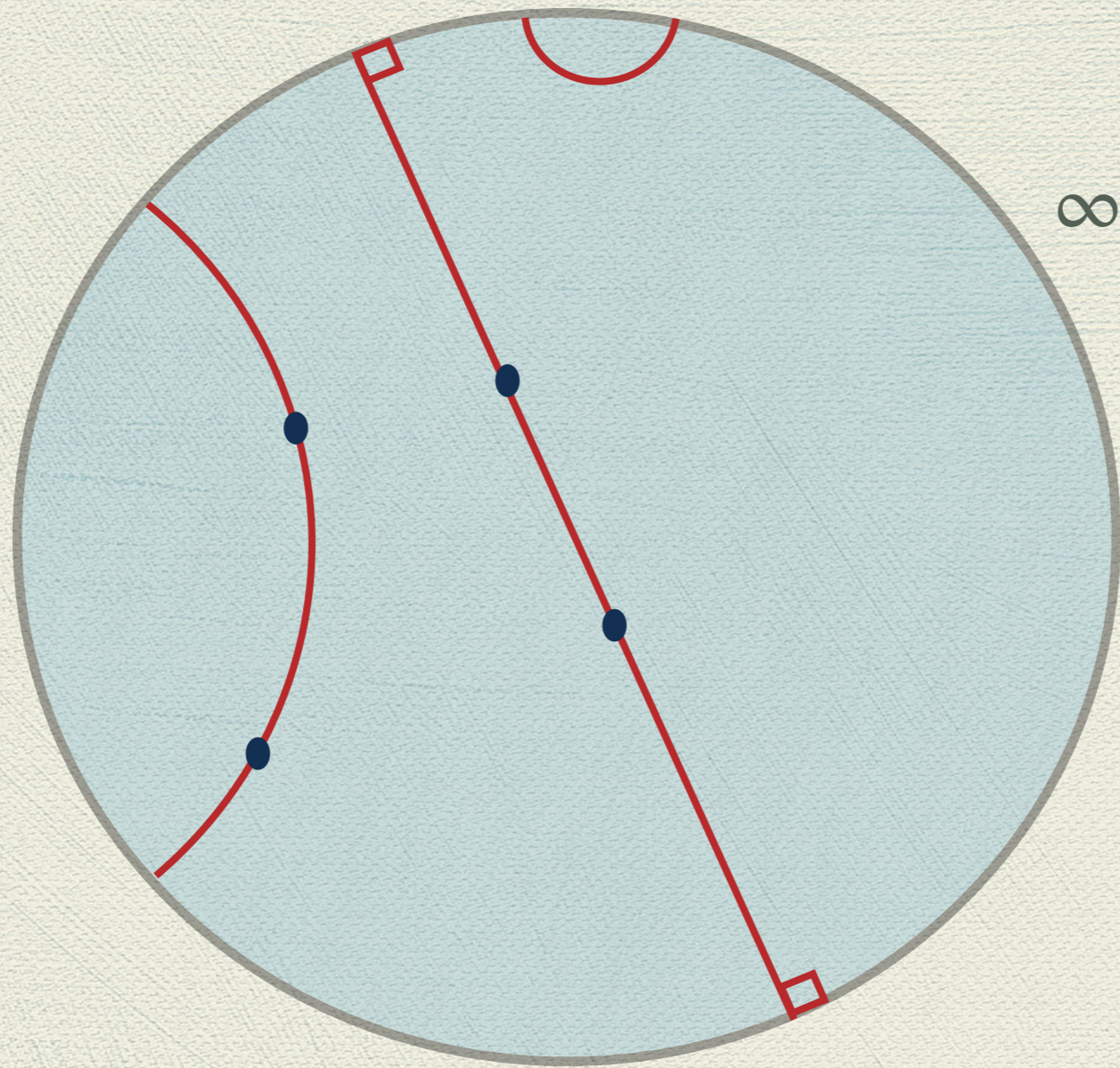


اصل موضوع پنجم در طول ۲۰۰۰ سال:

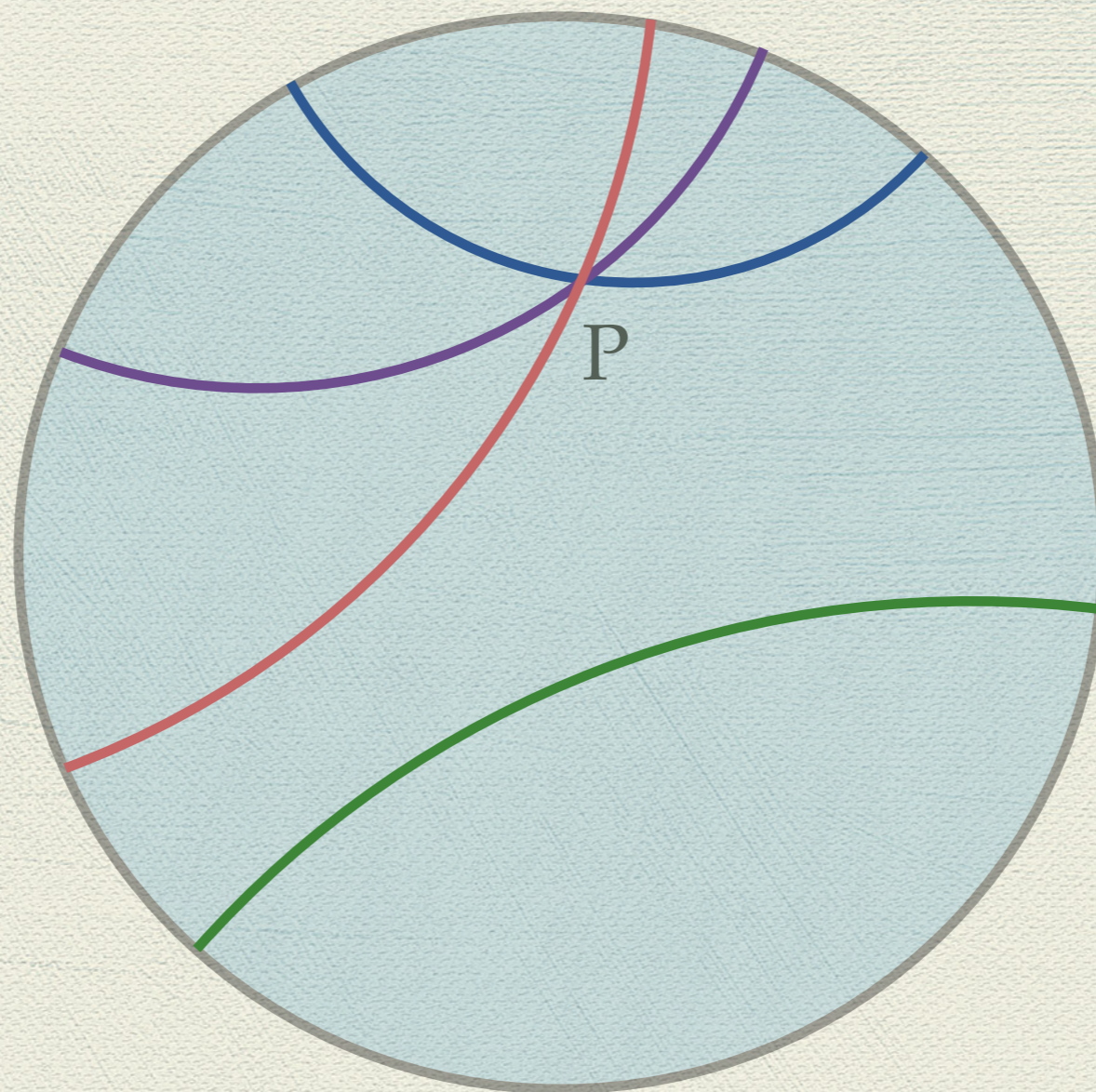
- از یک نقطه خارج یک خط تنها یک خط می توان به موازات آن رسم کرد.
- مجموع زوایای یک مثلث دو قائمه است.
- مثلثی وجود دارد که مجموع زاویه هایش دو قائمه است.
- هر مثلثی را در یک دایره می توان محاط کرد.
- مربعی وجود دارد که همه زاویه هایش قائمه هستند.
- دو خط که با خط سوم موازی باشند، خودشان با هم موازی اند.
- هیچ حد بالایی برای مساحت یک مثلث وجود ندارد.

- Proclus (410-485),
- Ibn al-Heytham (965-1039),
- Omar Khayyam (1050-1123),
- Nasir al-Din Tusi (1201-1274),
- Sadr al Din (1298),
- Girolamo Saccheri (1667-1733),
- Giordano Vitale (1633-1711),
- John Lambert (1766),
- Nikolai Lobachevsky (1829),
- Janos Bolyai (1831),
- Gauss,
- Reimann,...

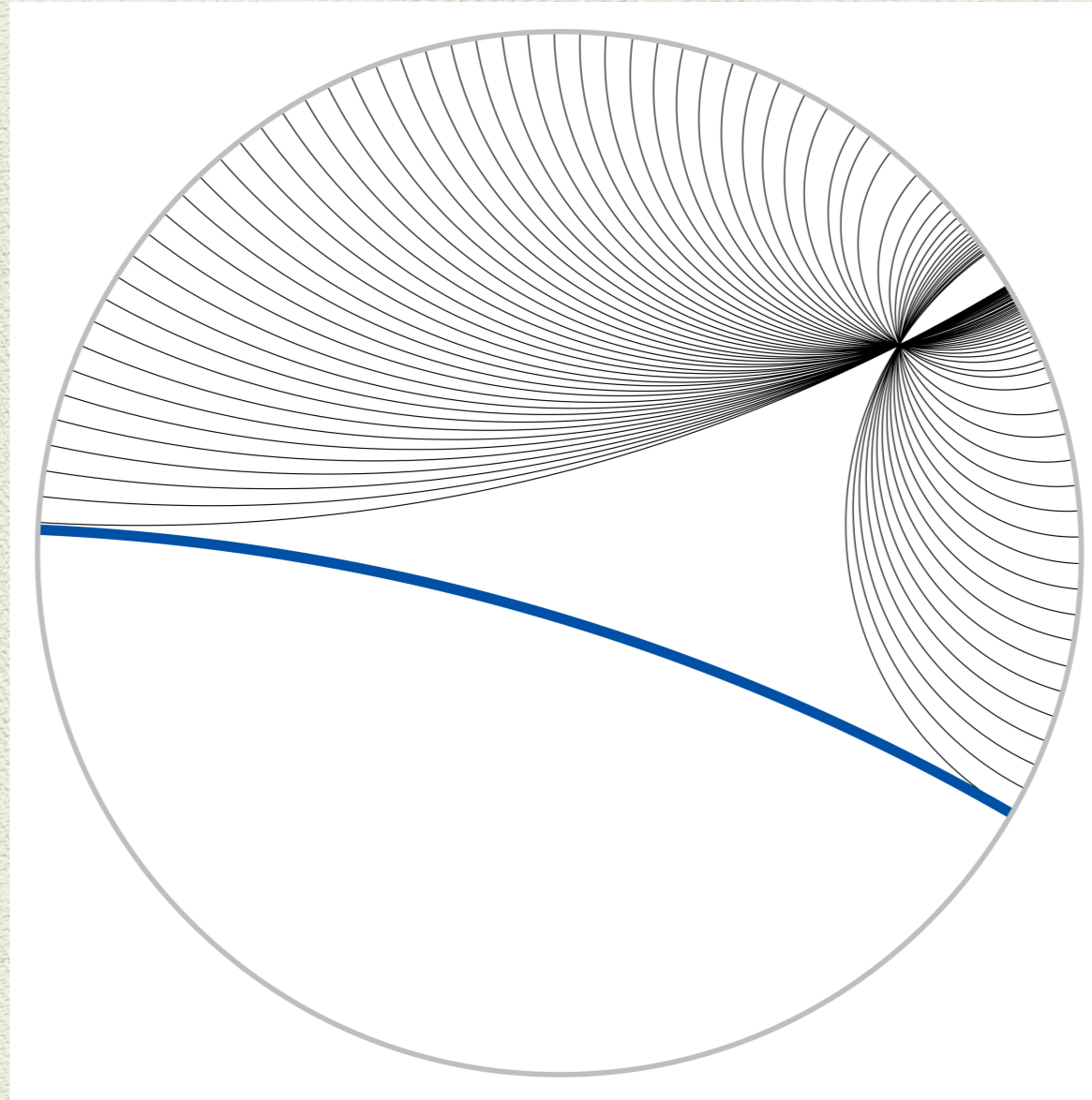
Hyperbolic Geometry



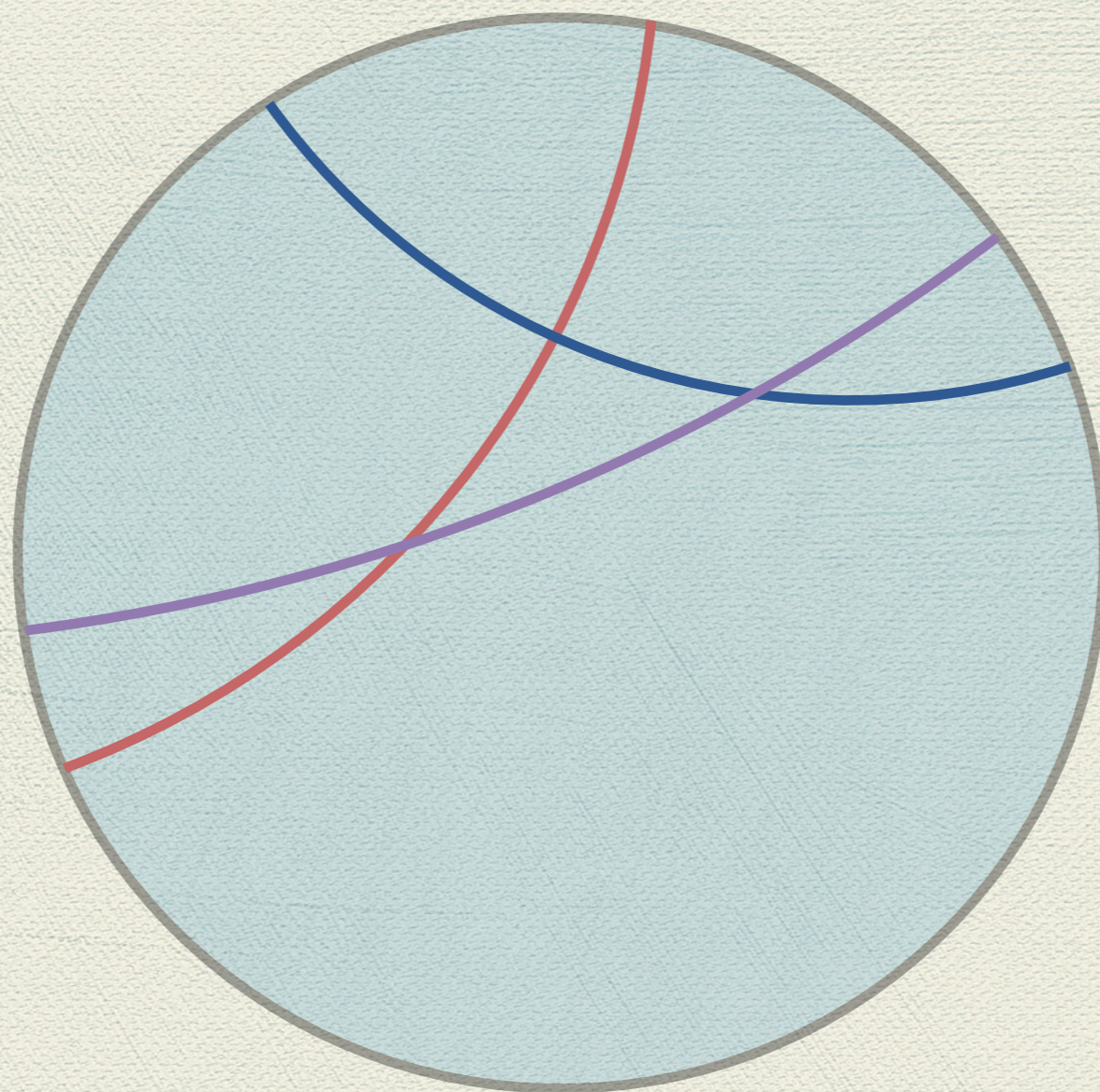
8



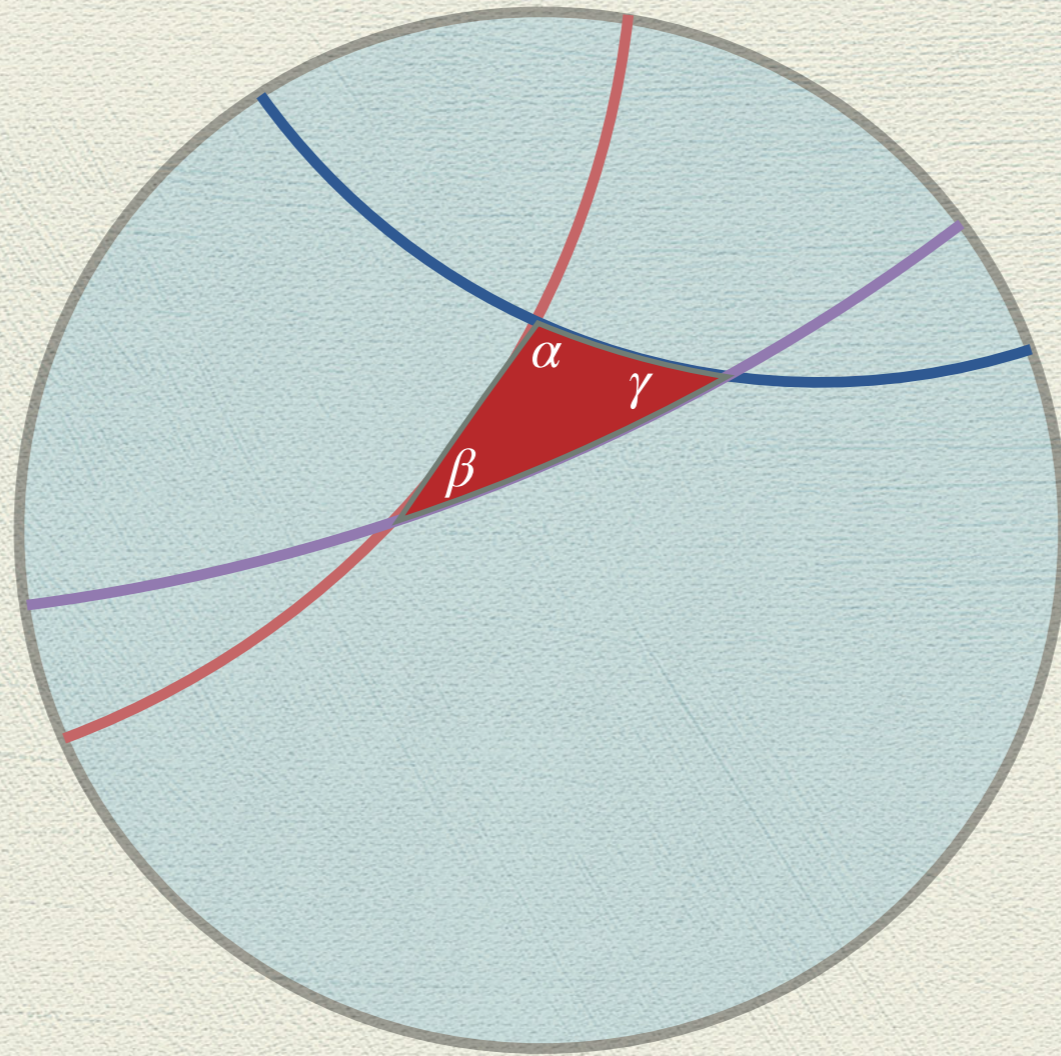
بر خلاف اصل پنجم اقلیدس:
از هر نقطه خارج یک خط بی نهایت خط عبور می کند که همه با آن خط موازی هستند.



بر خلاف اصل پنجم اقلیدس:
از هر نقطه خارج یک خط بی نهایت خط عبور می کند که همه با آن خط موازی هستند.



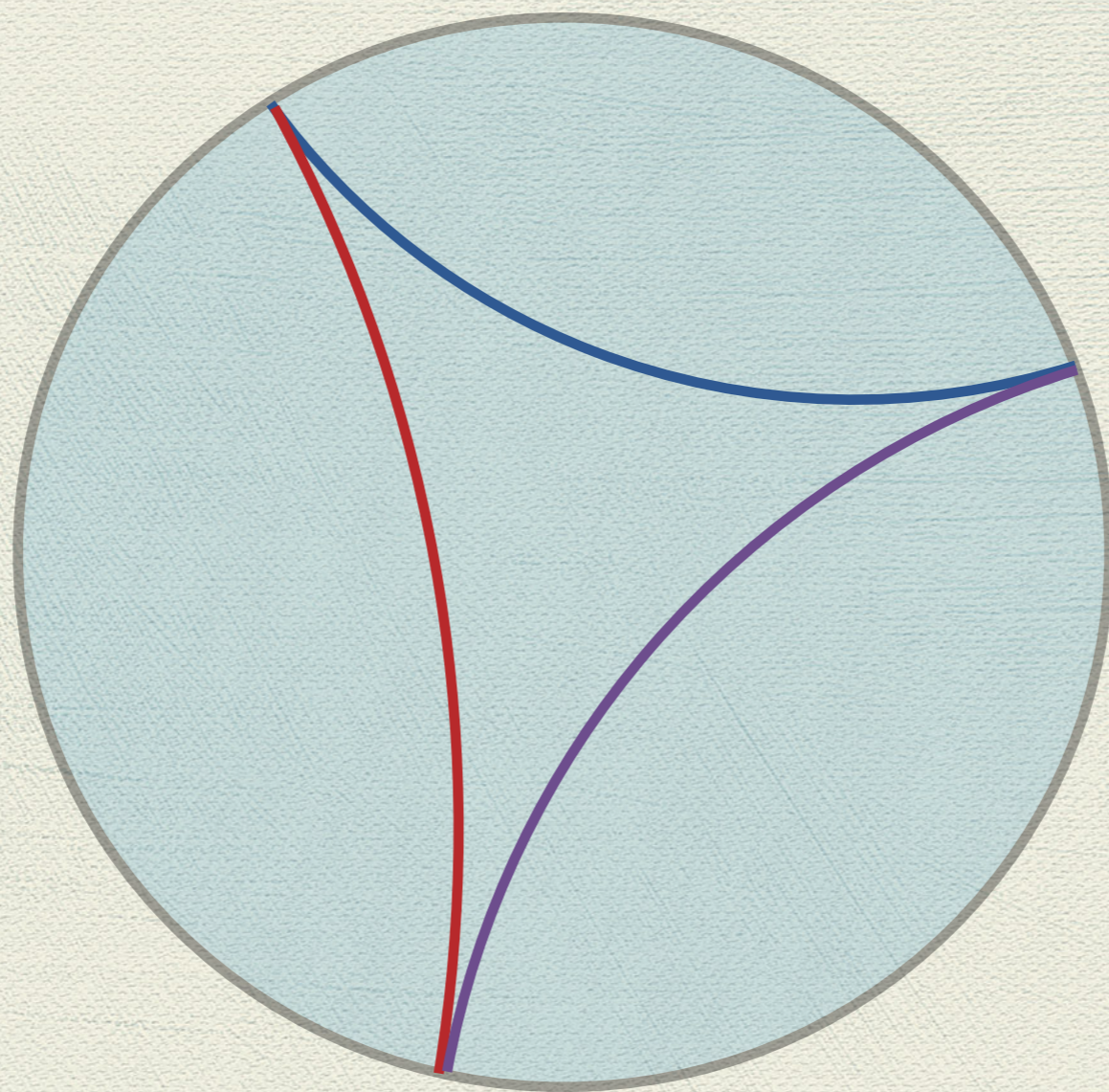
مجموع زوایای داخل یک مثلث کمتر از 180° درجه است.



مساحت یک مثلث

$$S = R^2(\pi - \alpha - \beta - \gamma)$$

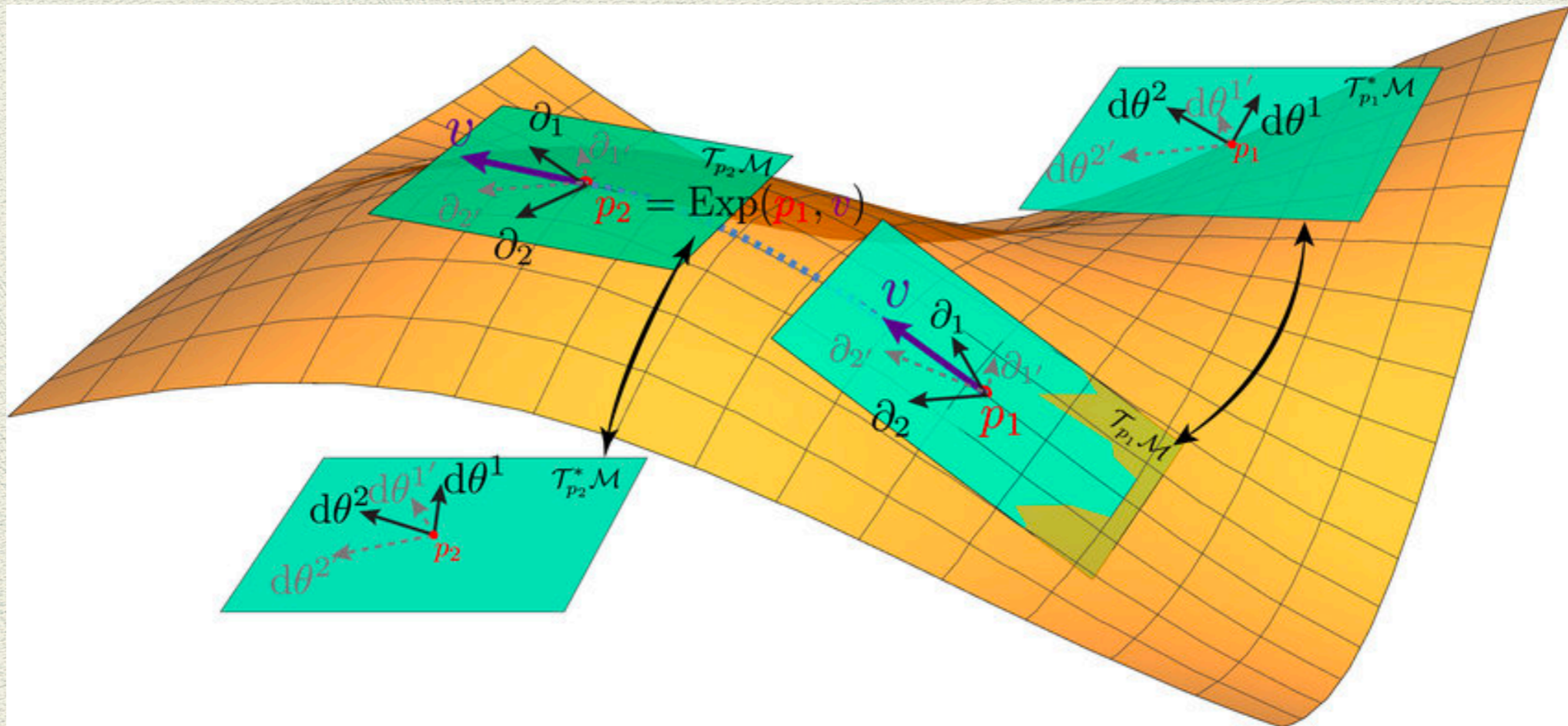
$$\alpha + \beta + \gamma \leq \pi$$



$$\alpha + \beta + \gamma = 0$$

$$S = \pi R^2$$

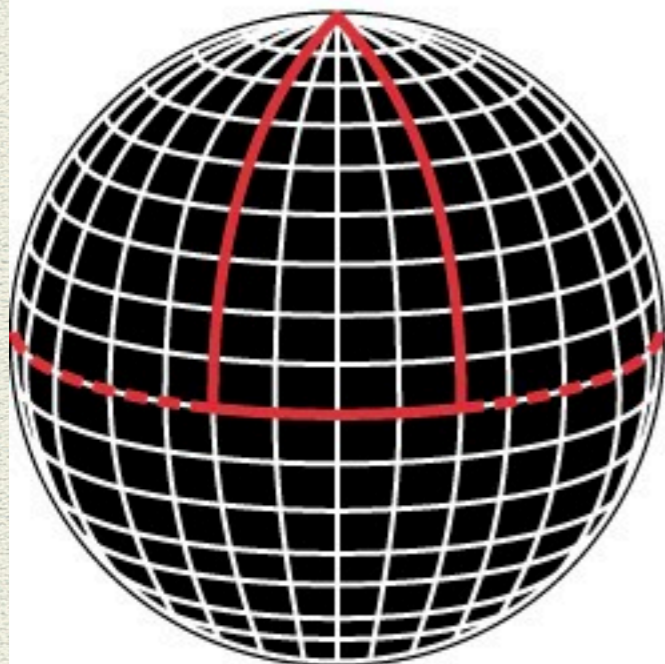
Riemannian Geometry



$$ds^2 = g_{\mu\nu} du^\mu du^\nu$$

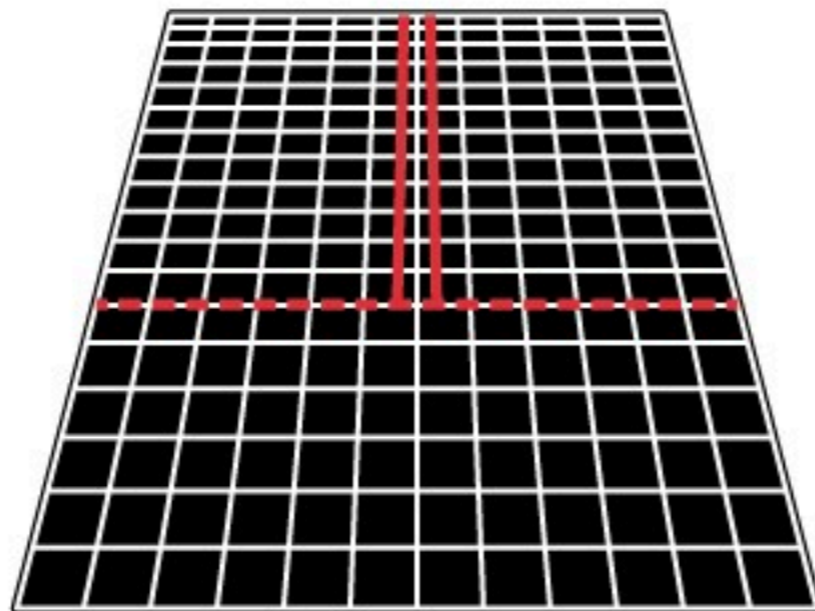
Spaces of Constant Curvature with Euclidean metric

Spherical space



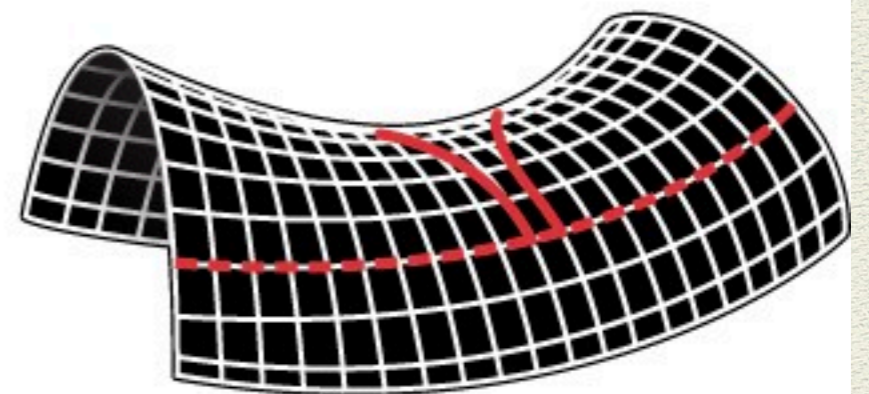
$$R > 0$$

Flat space



$$R = 0$$

Hyperbolic space

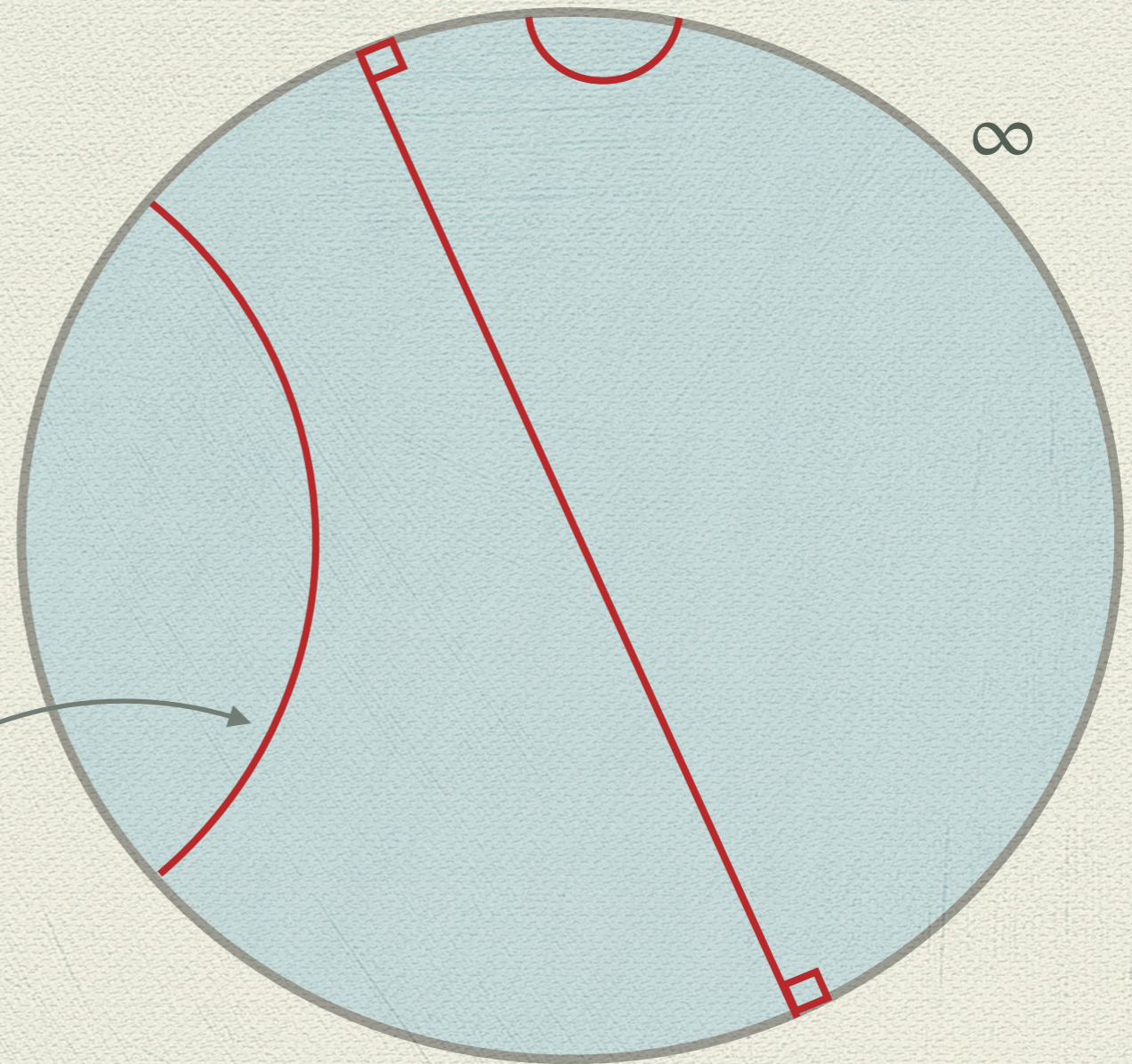


$$R < 0$$

Poincare Disk Model

$$ds^2 = \frac{4(dx^2 + dy^2)}{[1 - (x^2 + y^2)]^2}$$

Geodesics



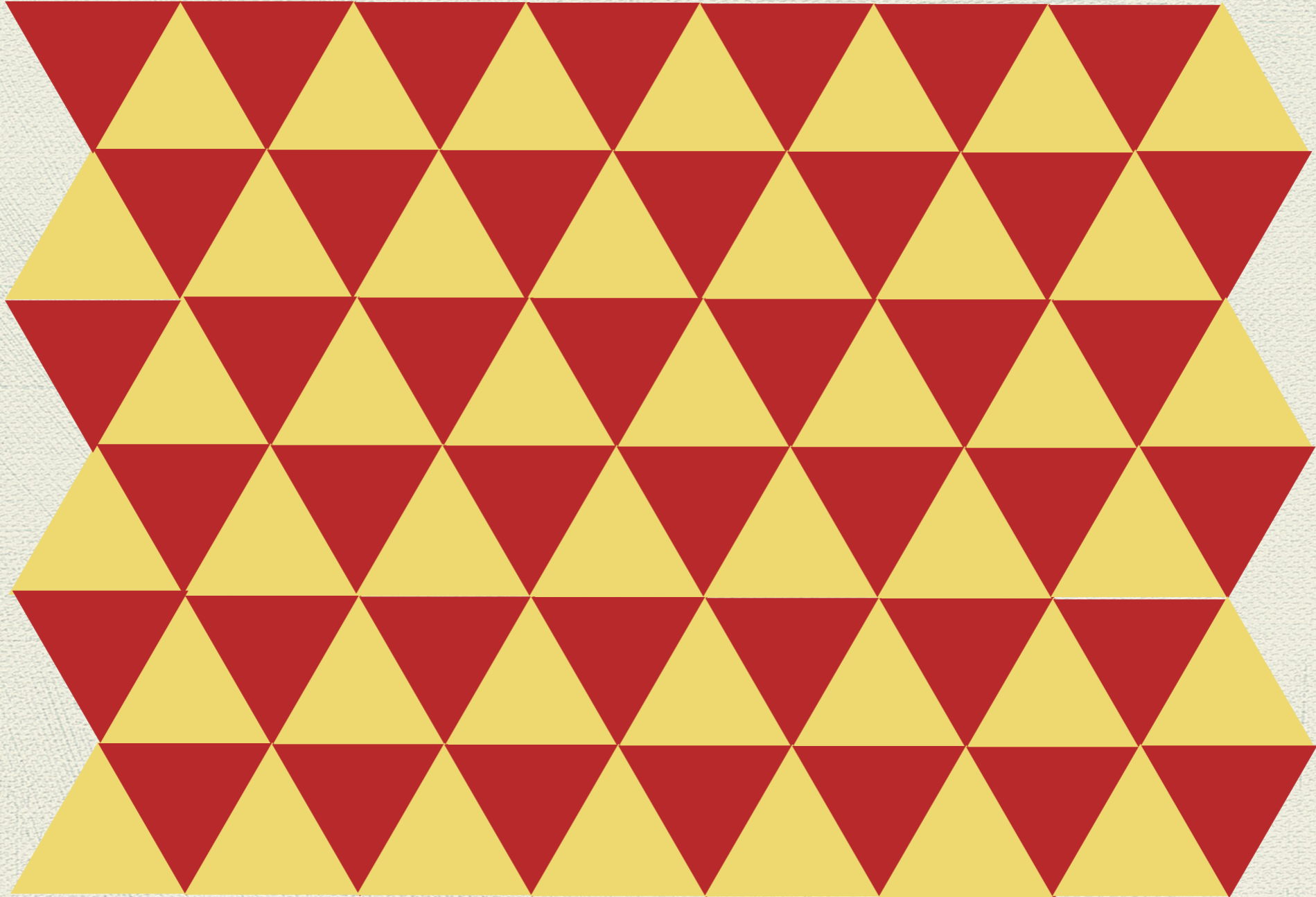
Euclidean Tessellations

یک سطح اقلیدسی را تنها به سه صورت می توان کاشی کاری کرد.

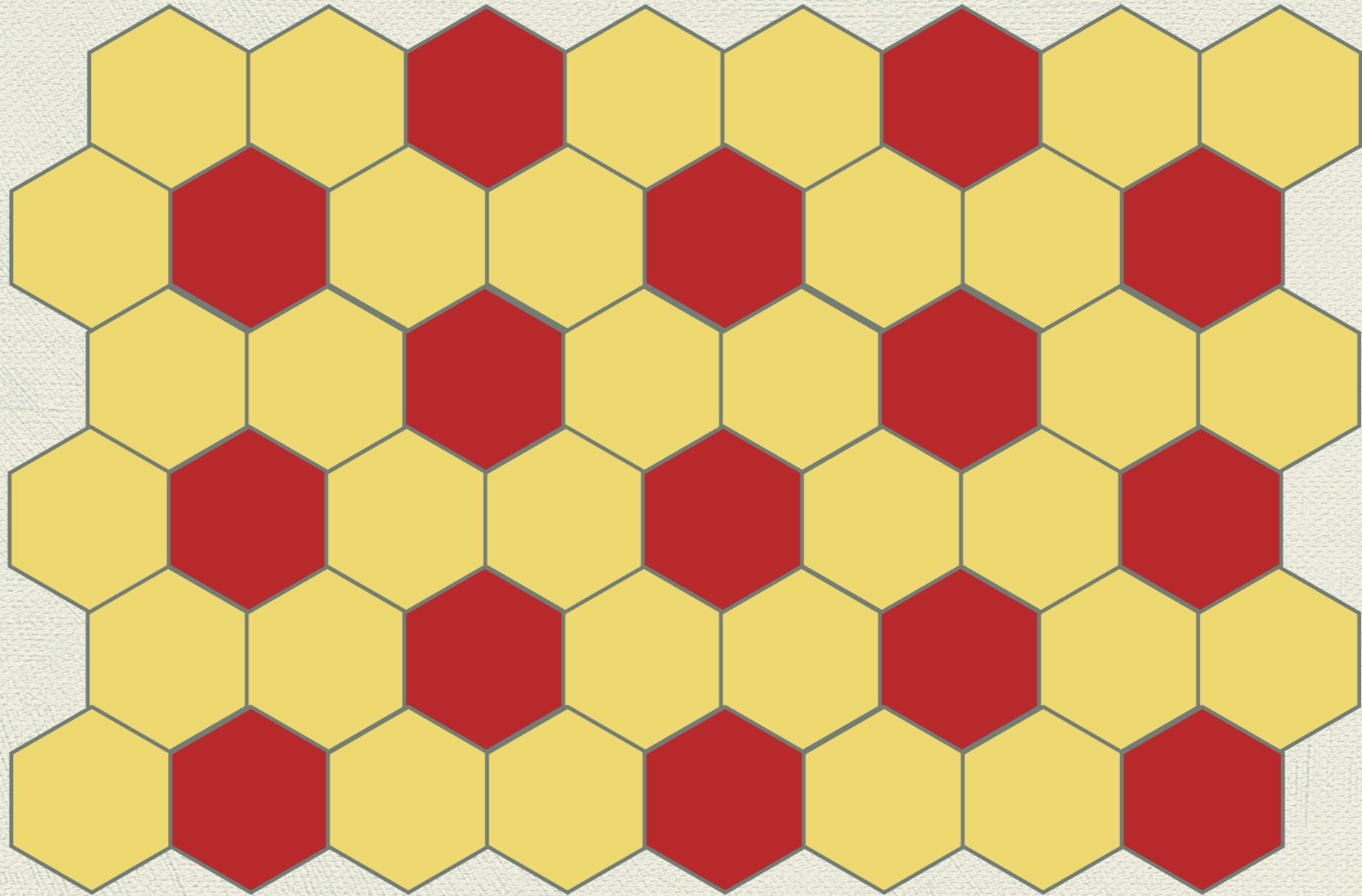
با مربع



با مثلث



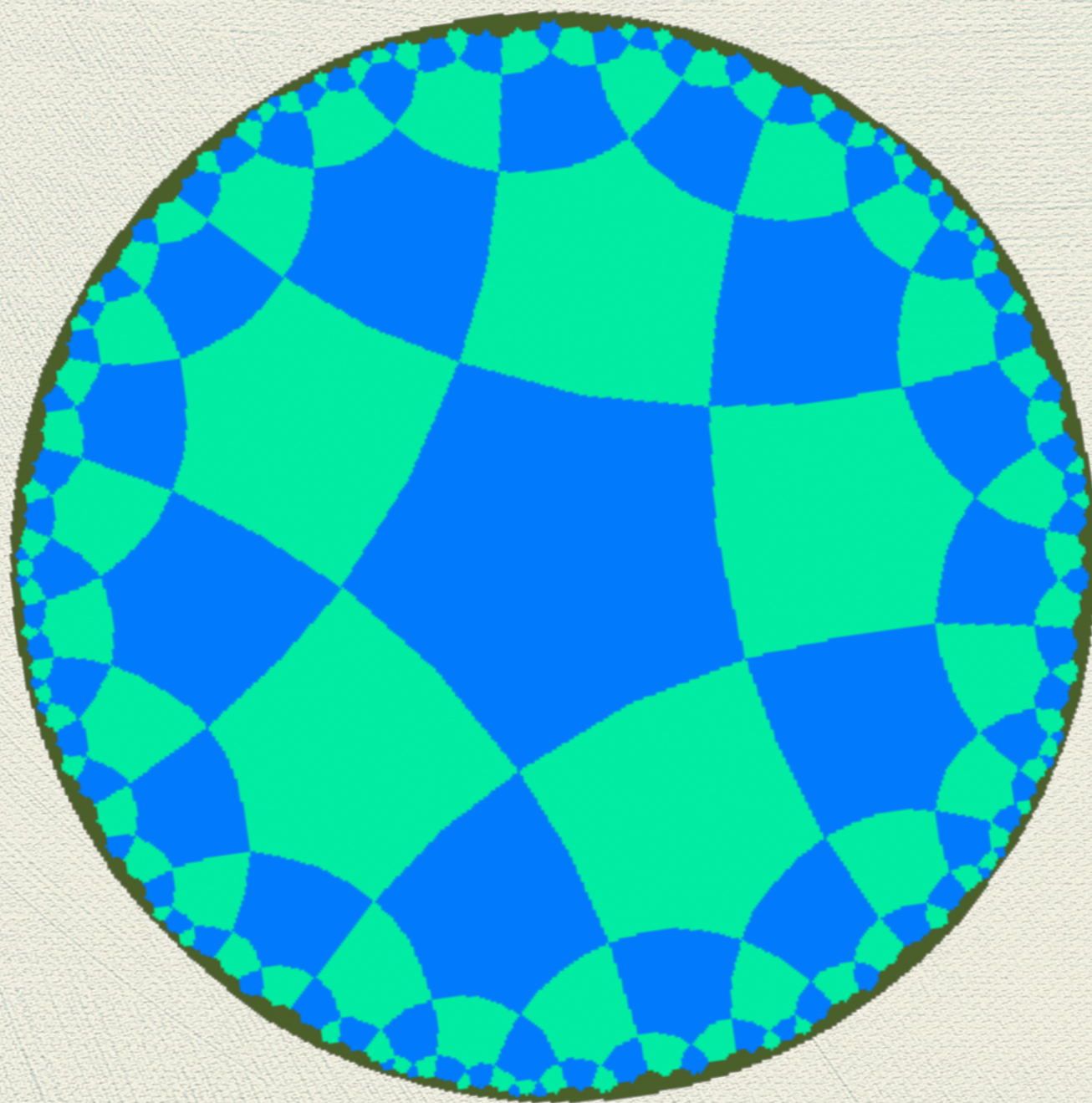
با شش ضلعی



Hyperbolic Tessellations

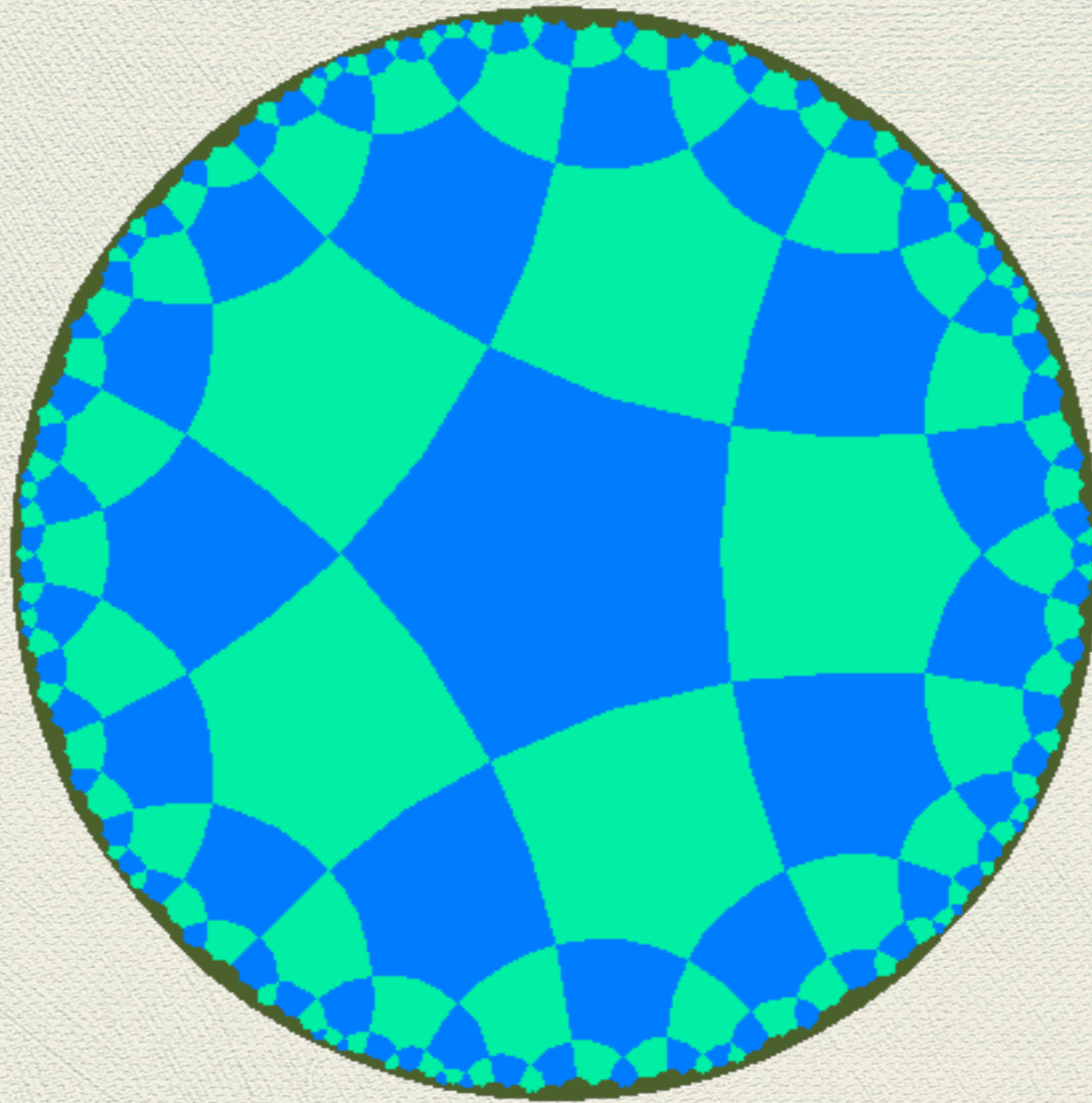
یک صفحه هذلولوی را به بی نهایت صورت می توان کاشیکاری کرد.

تمام این چند ضلعی ها یک اندازه هستند.

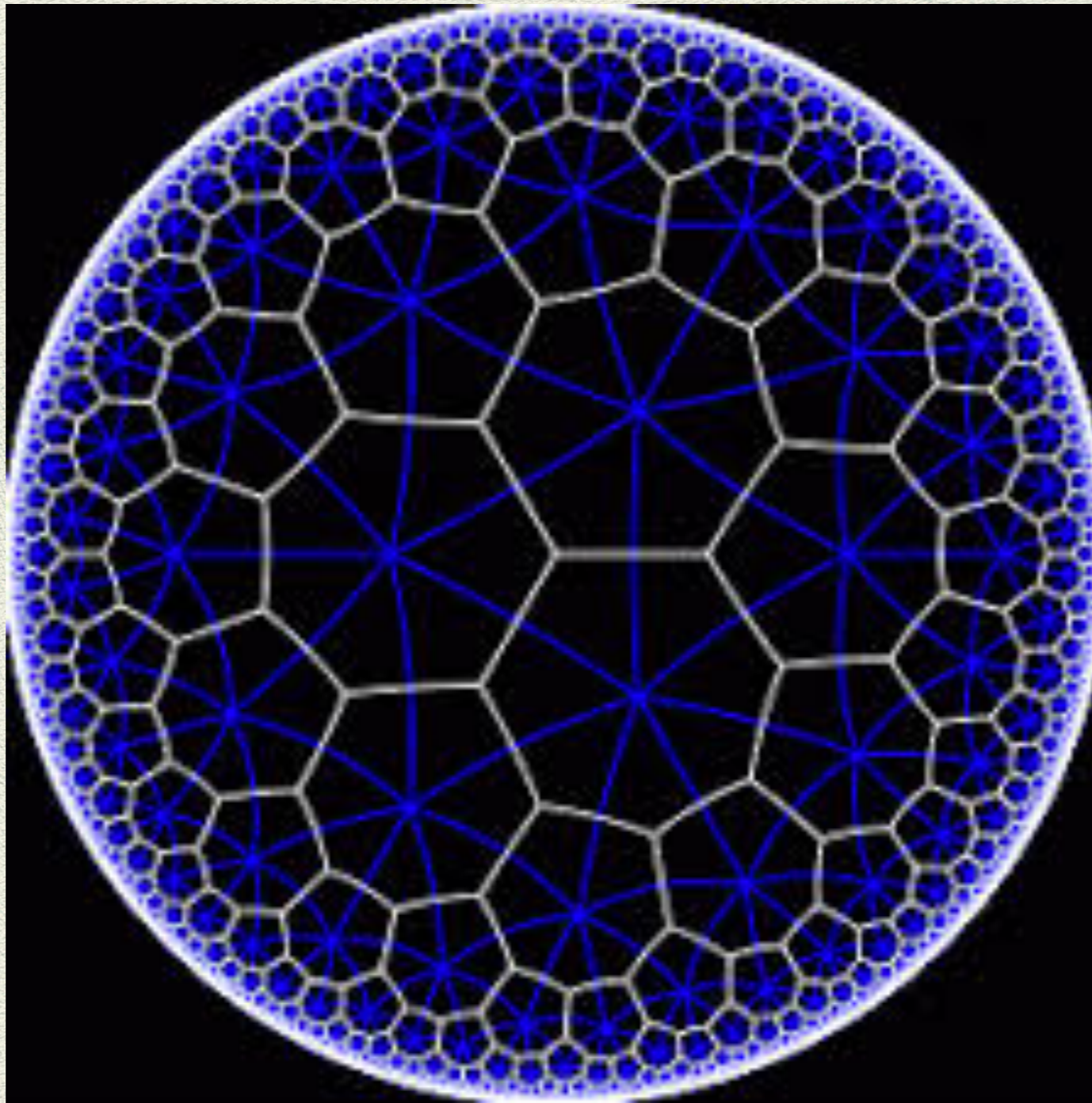


Schlaflfli Symbol = (5 , 4)

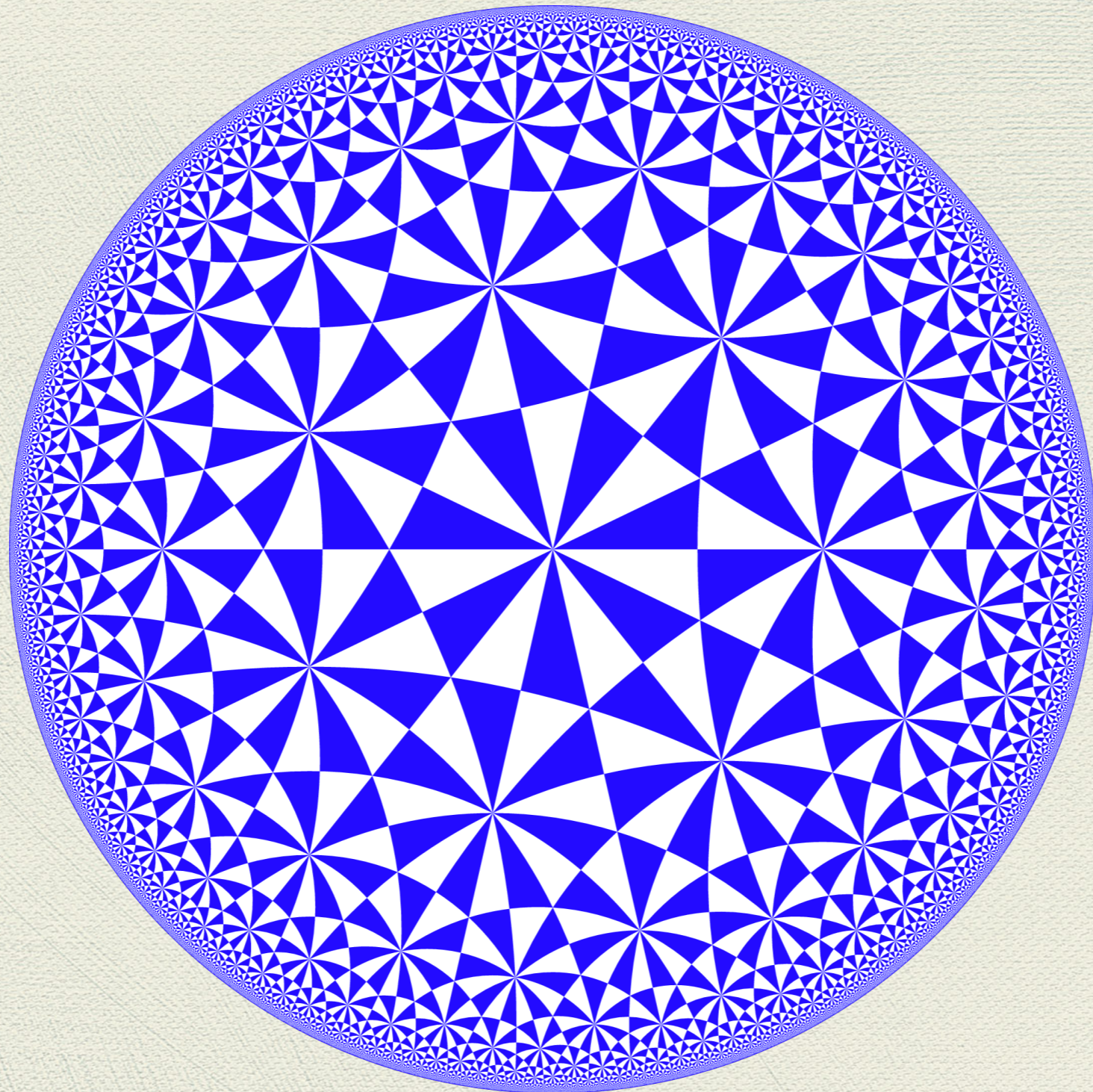
Regular Hyperbolic Tessellations



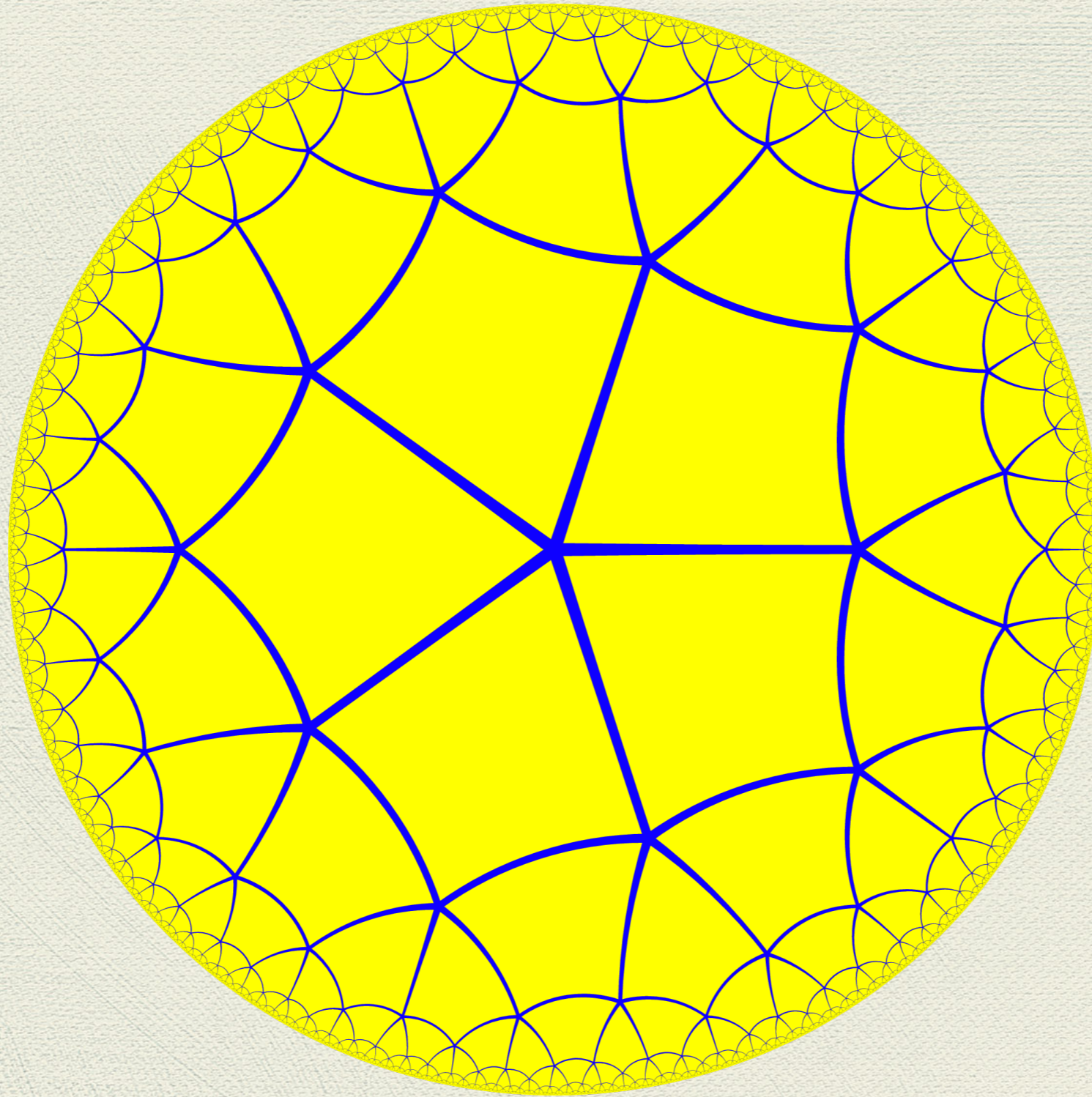
Schläfli Symbol = $(5, 4)$



Schlaflli Symbol = (6 , 3)



Schlaflfli Symbol = (3, 14)



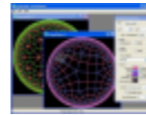
Schlaflli Symbol = (4 , 5)

Categories

Audio	14
Image editing / photo software	17
Operating systems	6
Security software	23
Browsers	7
Communication	8
Data storage	7
Download programs	4
Education	5
E-mail	11
Games	6
Hobby and read	11
Office software	23
Mobile apps	9
Video	12
Website development	26
Business software	13

Popular programs

ADPHONE	Happy Fish
Verge	Destructivator
Smart Mouse Share	jPDF Fields
Outlook Import Wizard	QB-US States
Monkeymen Desktop	Advanced IP Address
Calendar	Calculator
Functor	Easy Notes
Calendar Organizer	Real All Video
Deluxe	Converter
Remote Mail Cleaner	RecoveryFIX for PST



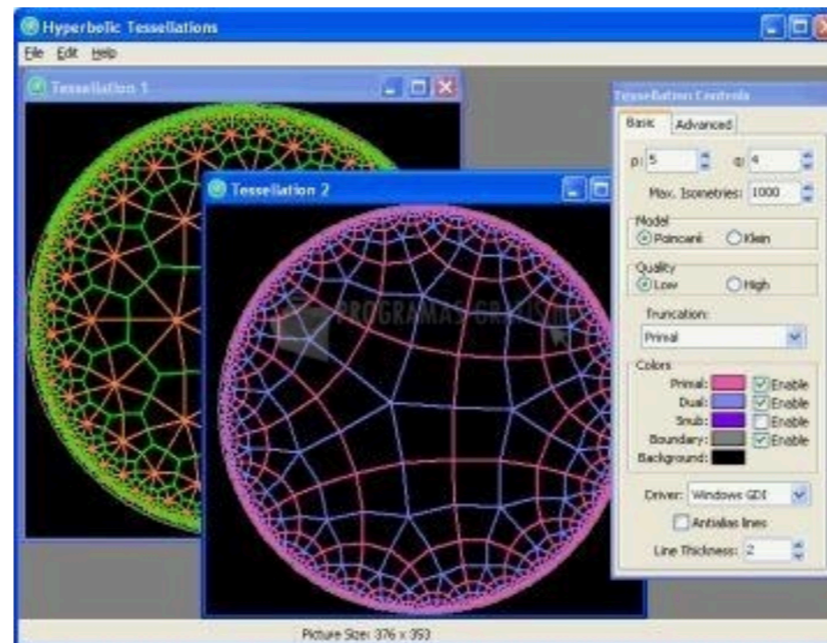
Hyperbolic Tessellations for Windows 10 32/64 download free



DOWNLOAD

With the name of. tessellations. (tessellations) we know a pattern of figures that completely covers or paves a flat surface in which there are no gaps and where the figures do not overlap. Examples: bathroom tiles, squares of linoleum on the floor of an office or street tiling.

Hyperbolic Tessellations is a tool that allows you to create an unlimited number of tessellations from the Menu, in File-> New. There you will find patterns. Choose one of them and take it through the drag and drop system to a hyperbolic space. In Hyperbolic Tessellations you can work with the right mouse button to edit the tessellations. In this way, you can specify the number of vertices to be drawn, the model, the quality, the color, and so on.

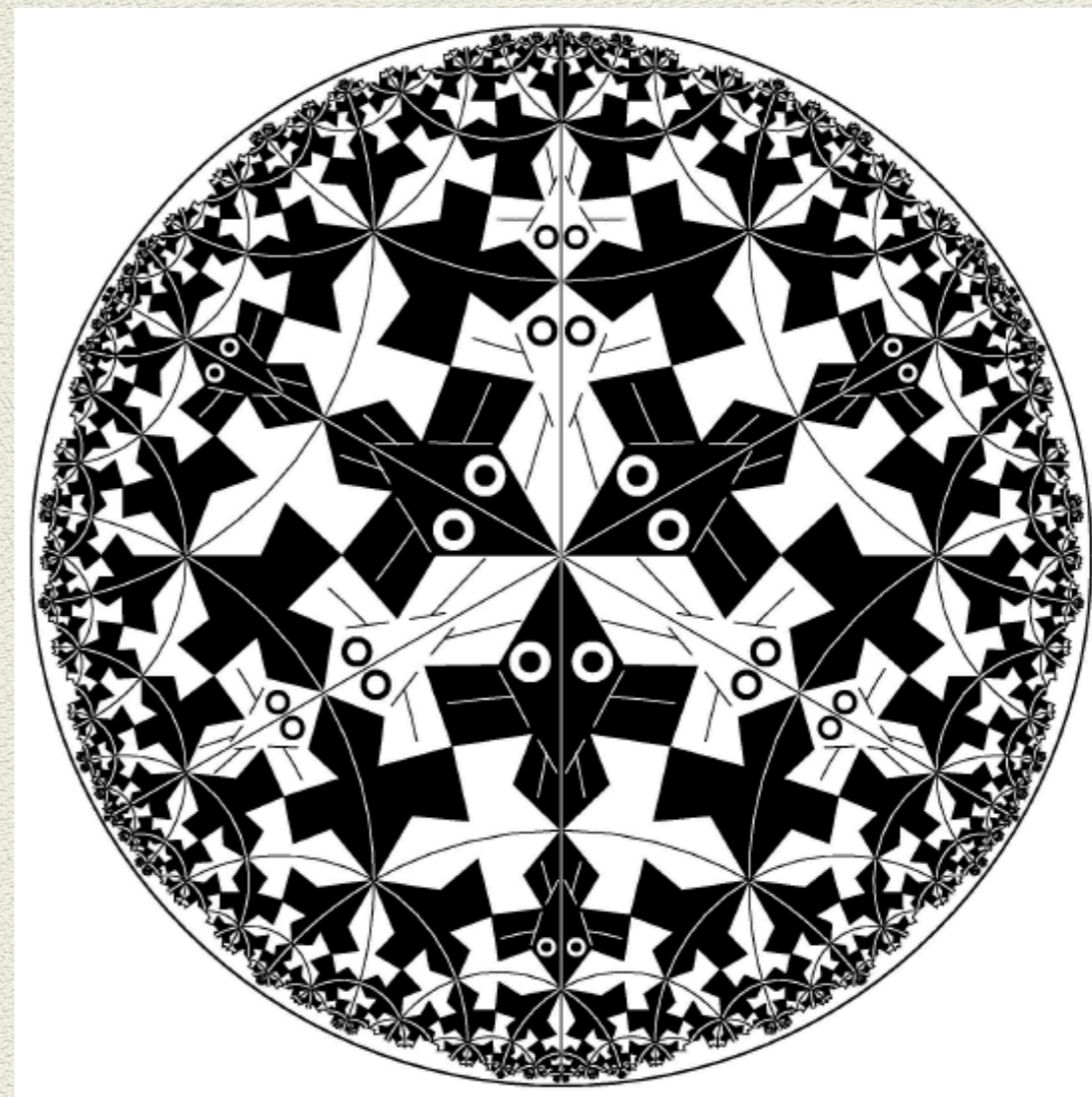
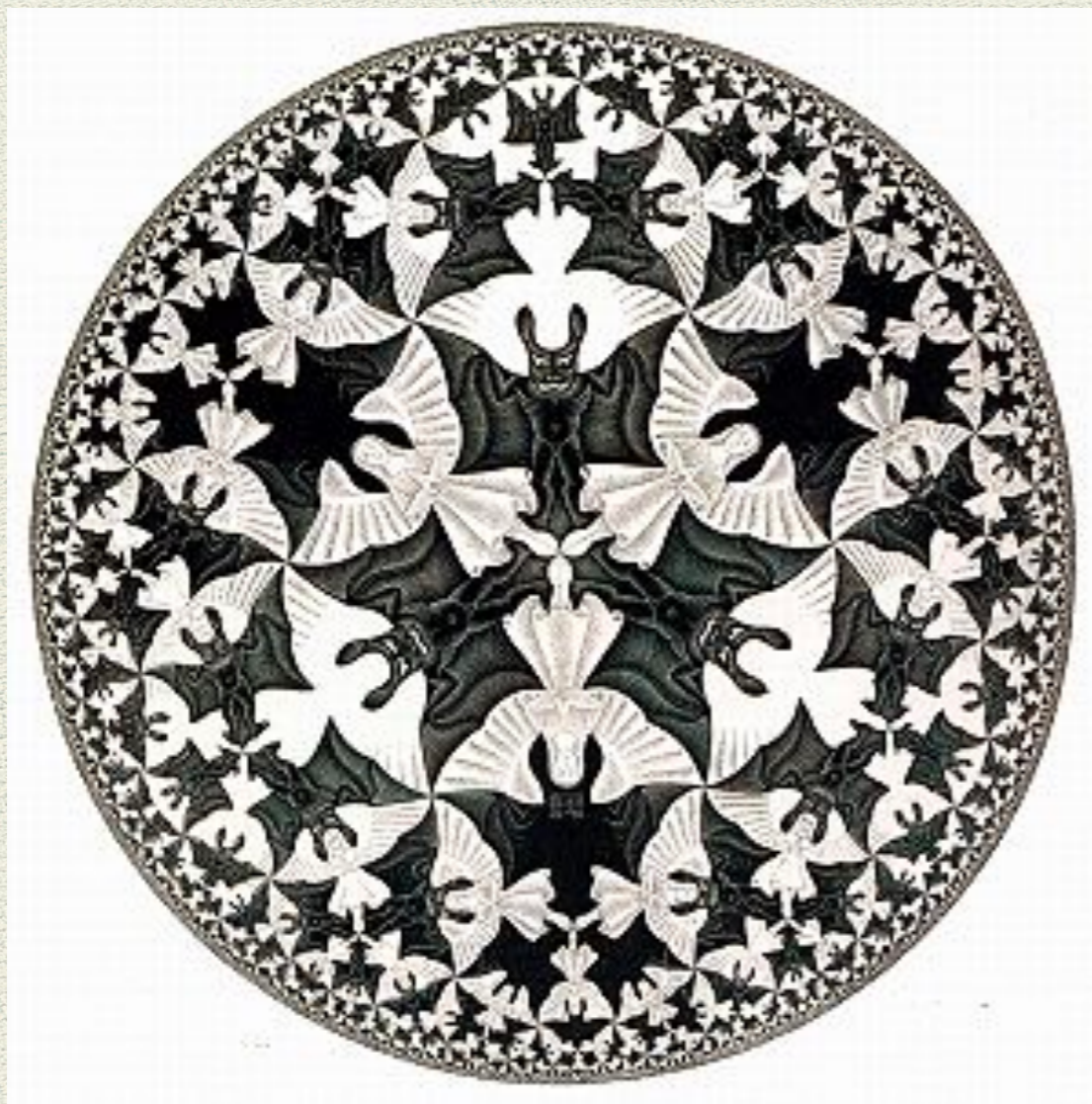


You can free download Hyperbolic Tessellations and safe install the latest trial or new full version for Windows 10 (x32, 64 bit, 86) from the official site.

Devices: Desktop PC, Laptop (ASUS, HP, DELL, Acer, Lenovo, MSI), Ultrabook

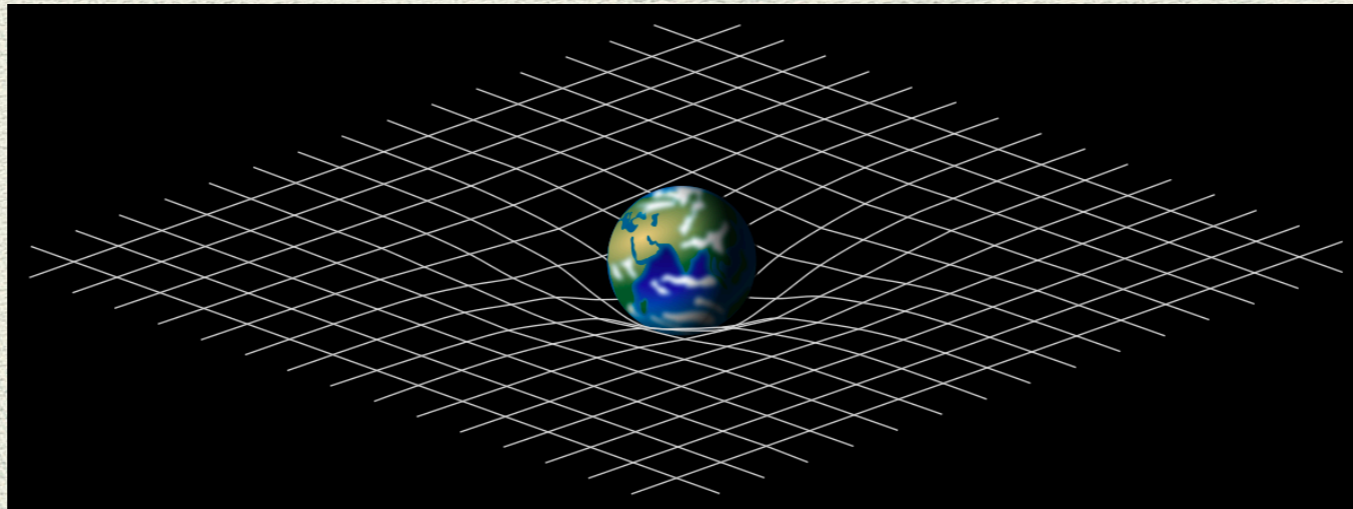
OS: Professional, Enterprise, Education, Home Edition, versions: 1507, 1511, 1607, 1703, 1709, 1803, 1809

Esher Artworks



Black Holes

Einstein's Equation

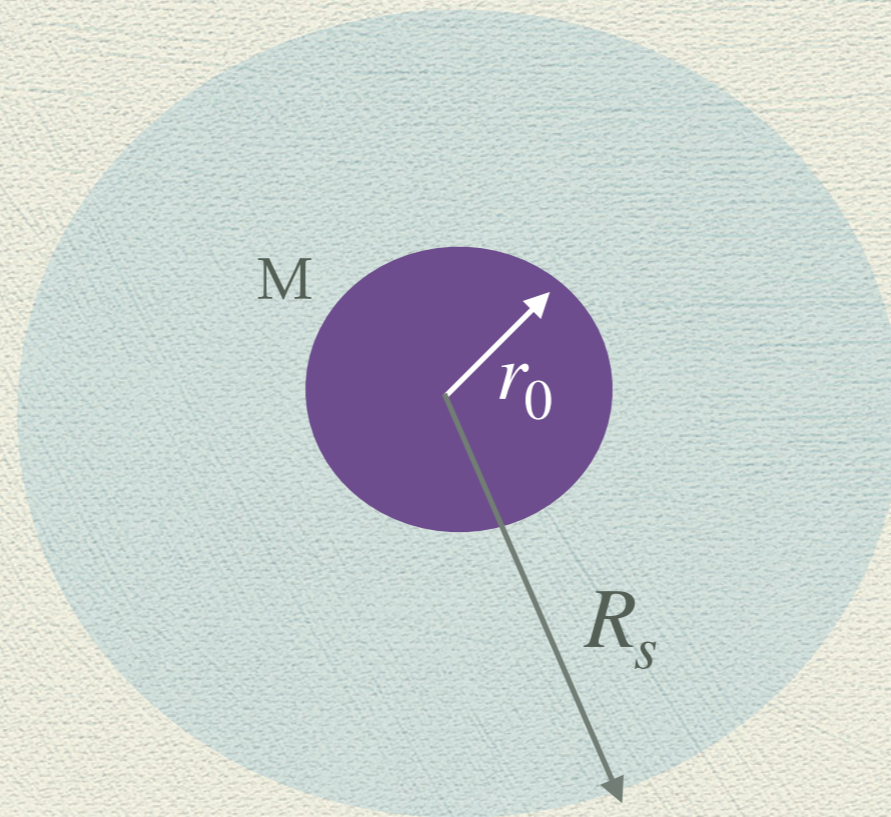


$$ds^2 = g_{\mu\nu} dx^\mu dx^\nu$$

$$G_{\mu\nu} = \frac{8\pi G}{c^3} T_{\mu,\nu}$$

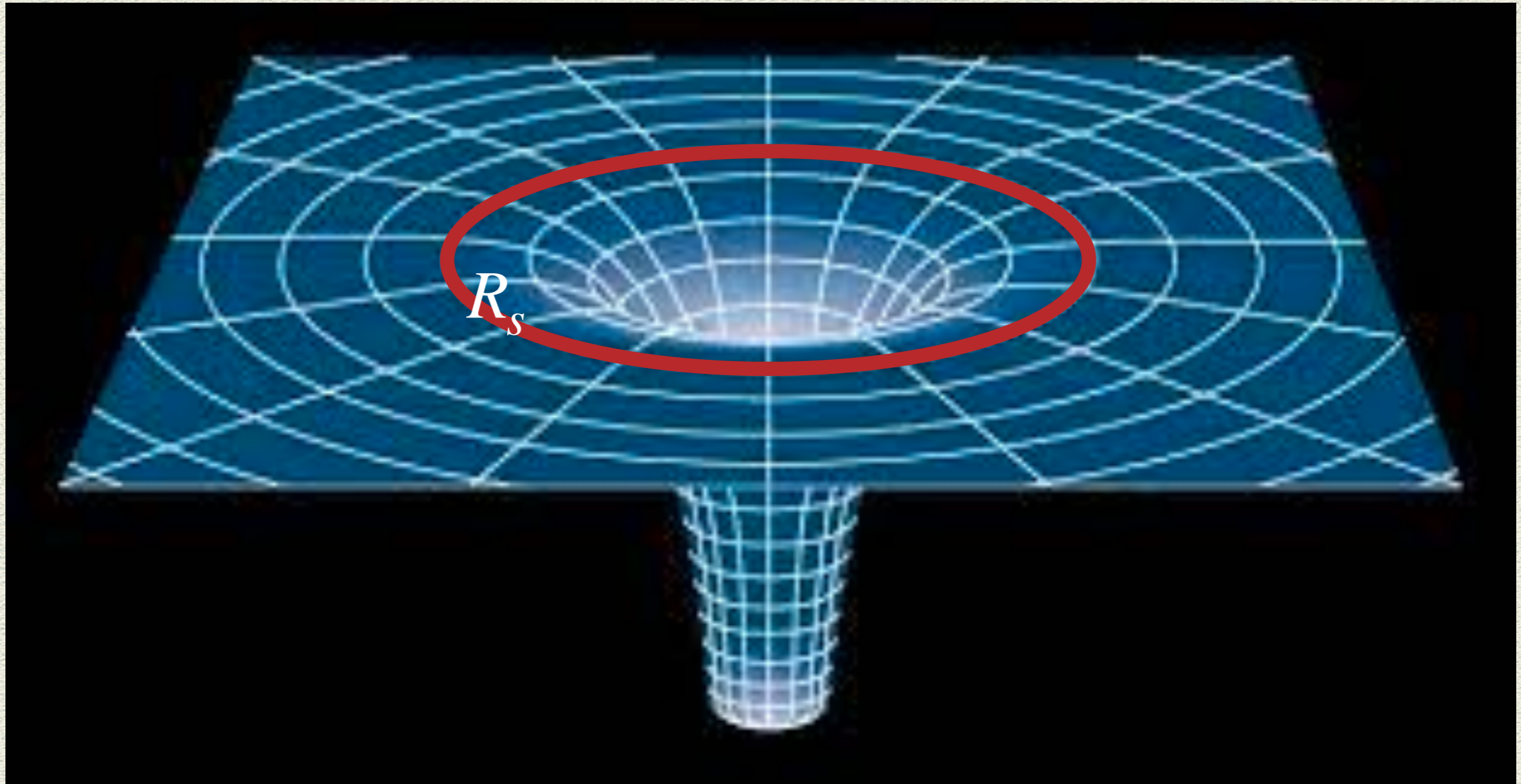
$$G_{\mu\nu} := R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R$$

Schwartzchild Solution



$$ds^2 = \left(1 - \frac{R_s}{r}\right)c^2 dt^2 - \frac{dr^2}{1 - \frac{R_s}{r}} - r^2 d\Omega^2$$

$$R_s = \frac{2GM}{c^2}$$



Black hole has no matter inside it

Singularity Theorems

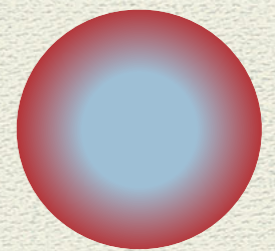
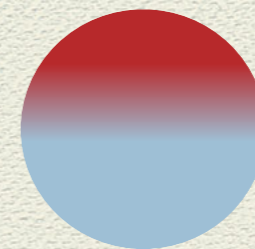


Roger Penrose and Steven Hawking

No Hair Theorem

The spacetime outside horizon depends only on
Mass (M), Charge (Q) and Angular Momentum (J)

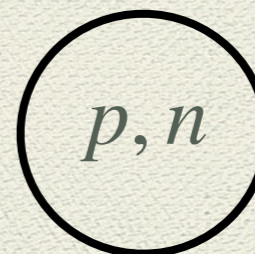
Independent of mass and charge distribution



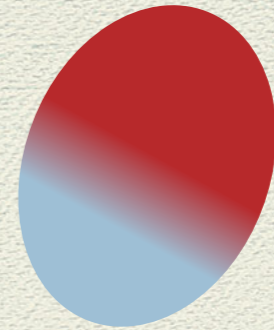
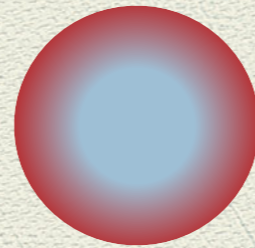
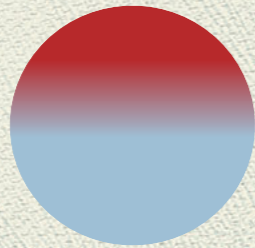
Independent of matter or anti-matter



Independent of baryon or lepton number

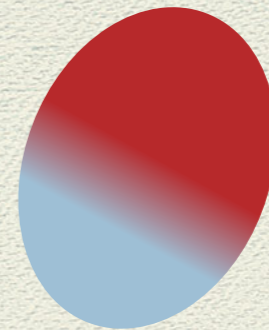
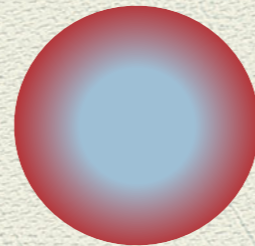
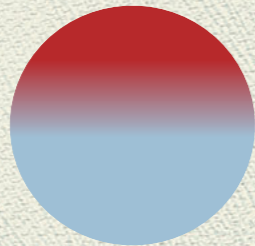


Why this is unexpected?

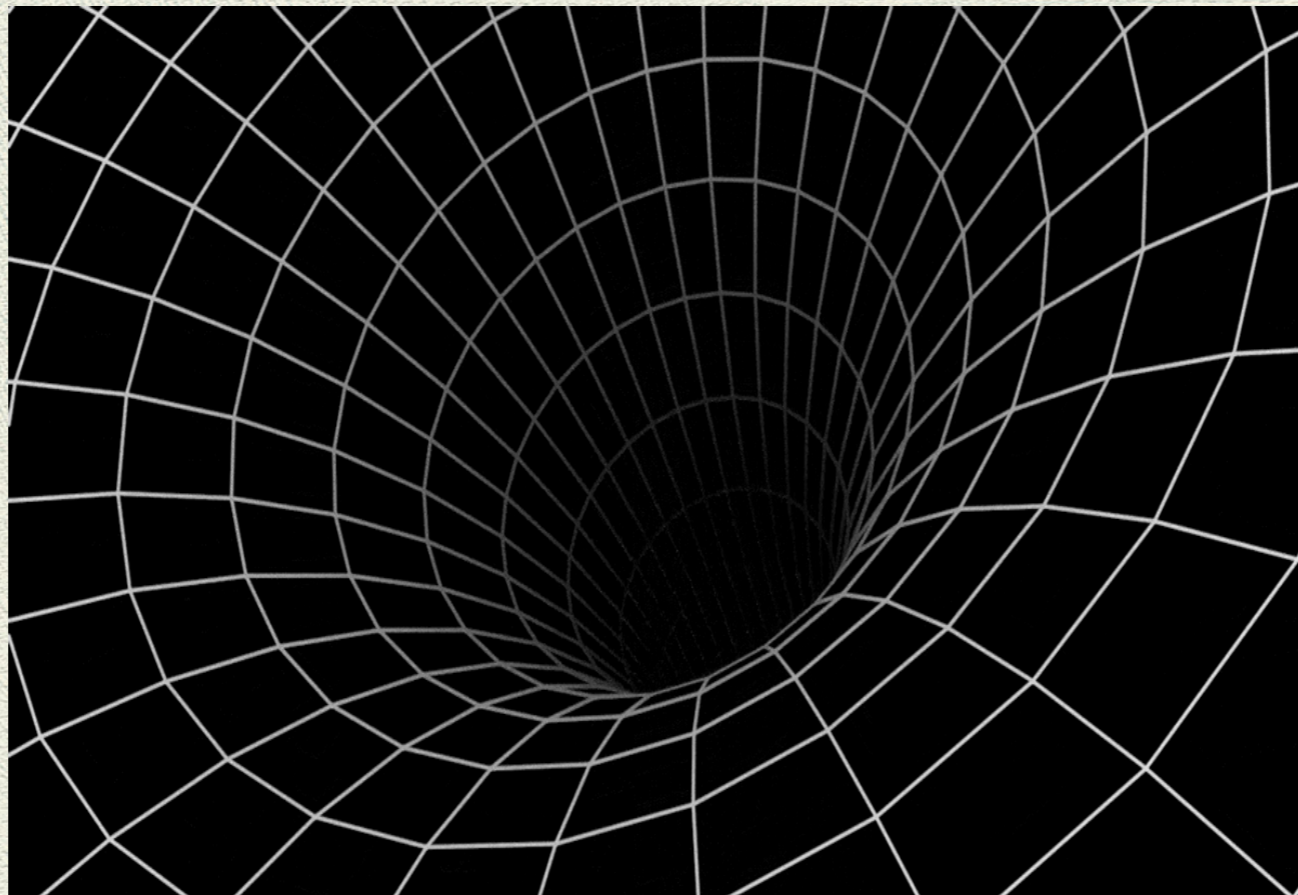
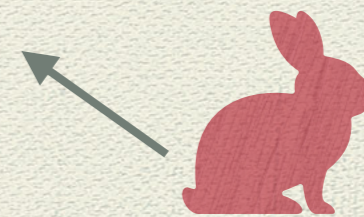
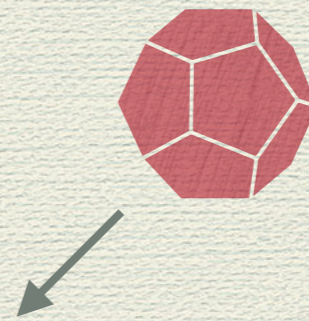


No matter how the matter collapses,
the final spacetime around the black hole does not depend on the
original distribution.

Why this is important?



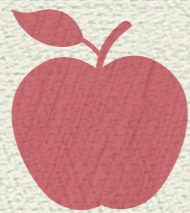
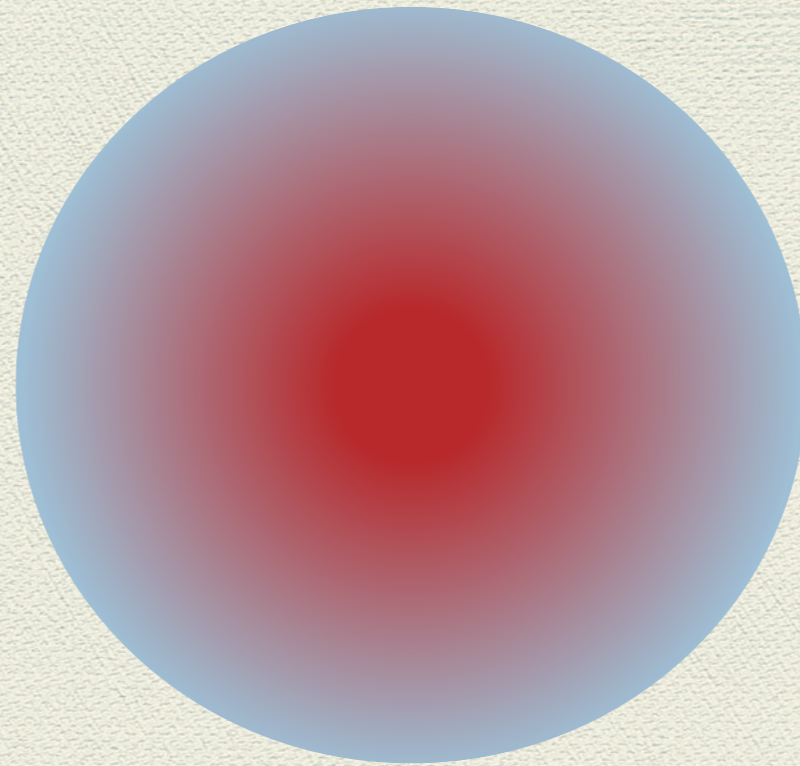
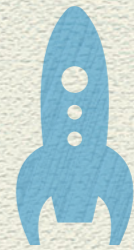
Because all the information is lost!



Conflict with Unitarity



Observer outside
horizon



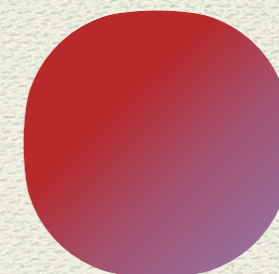
M

Q: Don't we have the same thing in everyday life?



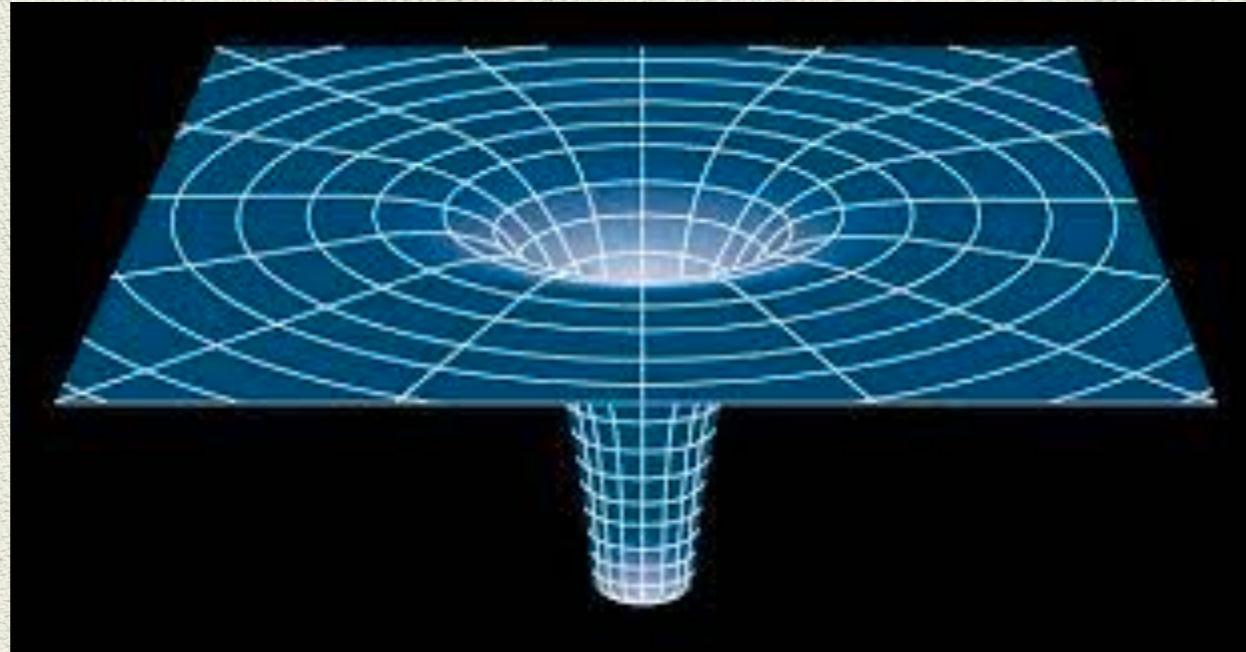
A: We are not talking about a multitude of particles.
This happens even at the microscopic level?

Q: Don't we have the same thing in quantum operations?



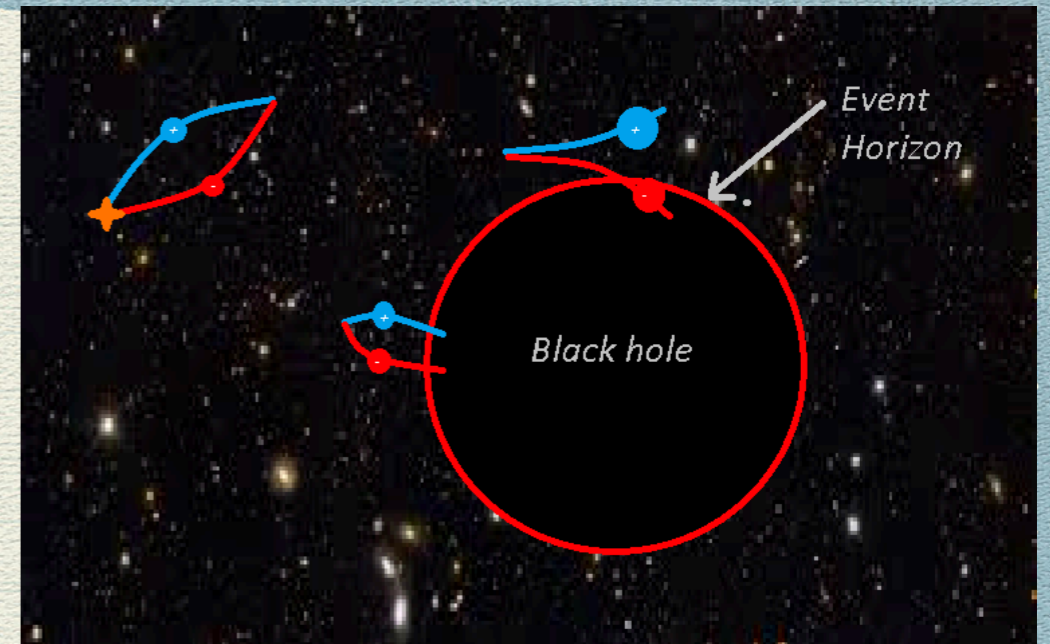
$$F(\mathcal{E}(\rho), \mathcal{E}(\sigma)) \geq F(\rho, \sigma)$$

A: Yes, but there is no environment here.



Any object + Black hole of mass m \longrightarrow Black hole of mass M

Moreover: Black hole evaporates!



1-Quantum Field Theory in curved space time

2-Extreme Gravity near the horizon
which changes virtual particles to real particles

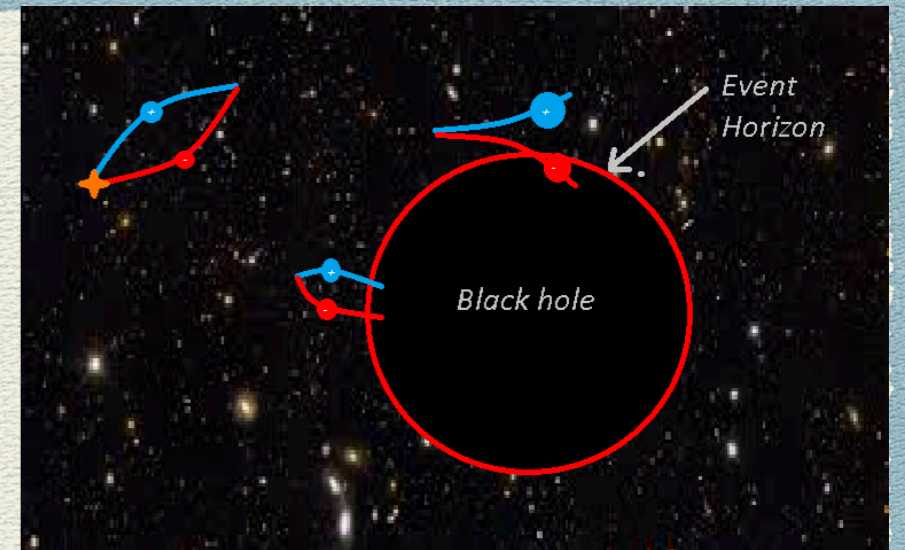
3-Entanglement



Hawking radiation

$$T = \frac{\hbar c^3}{8\pi G k M}$$

$$T = \frac{\hbar c^3}{8\pi G k M}$$



1-Large black holes are cooler

2-The black hole becomes hotter as it radiates

3-In natural units: $\hbar = c = G = k = 1$

$$T = \frac{1}{8\pi M}$$

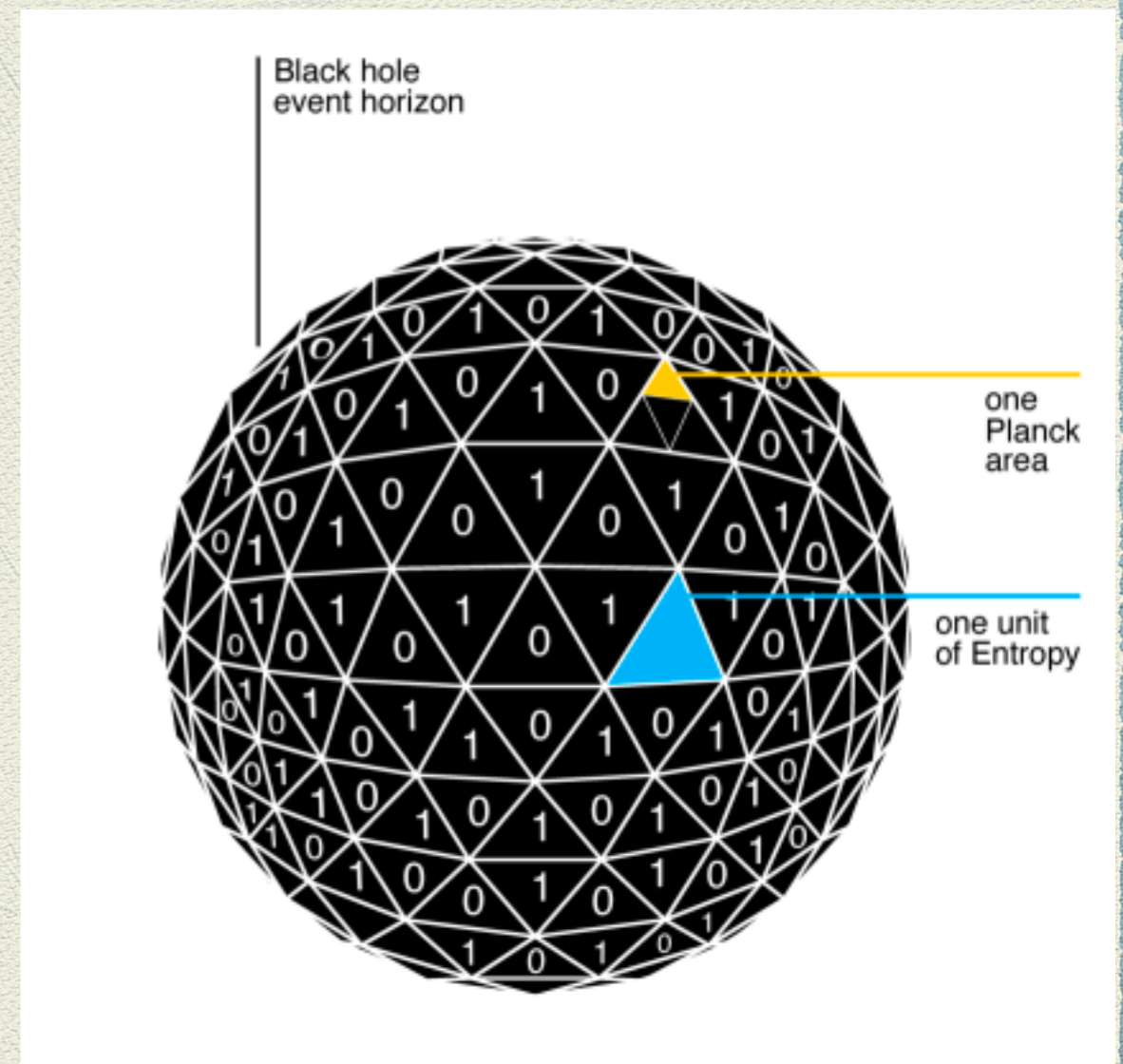
$$dS = \frac{dQ}{T} = 8\pi M dQ = 8\pi M dM$$

$$S = 4\pi M^2$$

$$S = 4\pi M^2$$

$$R_s = \frac{2GM}{c^2} \longrightarrow R_s = 2M \longrightarrow S = \pi R_s^2 \longrightarrow S = \frac{A}{4}$$

This result agrees with Beckenstein's bound



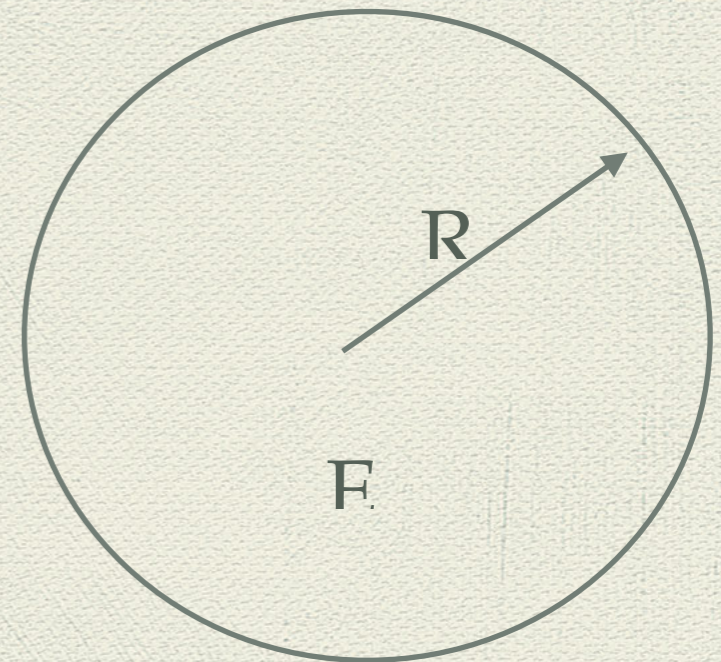
Beckenstein Bound

Quantum Field Theory in Curved Spacetime

Maximum entropy in any region of space $S \leq \frac{2\pi k R E}{\hbar c}$

$$I = \log \Omega = \frac{\ln \Omega}{\ln 2} = \frac{k \ln \Omega}{k \ln 2} = \frac{S}{k \ln 2}$$

$$I \leq \frac{2\pi R E}{\hbar c \ln 2}$$



The maximum information inside a black hole

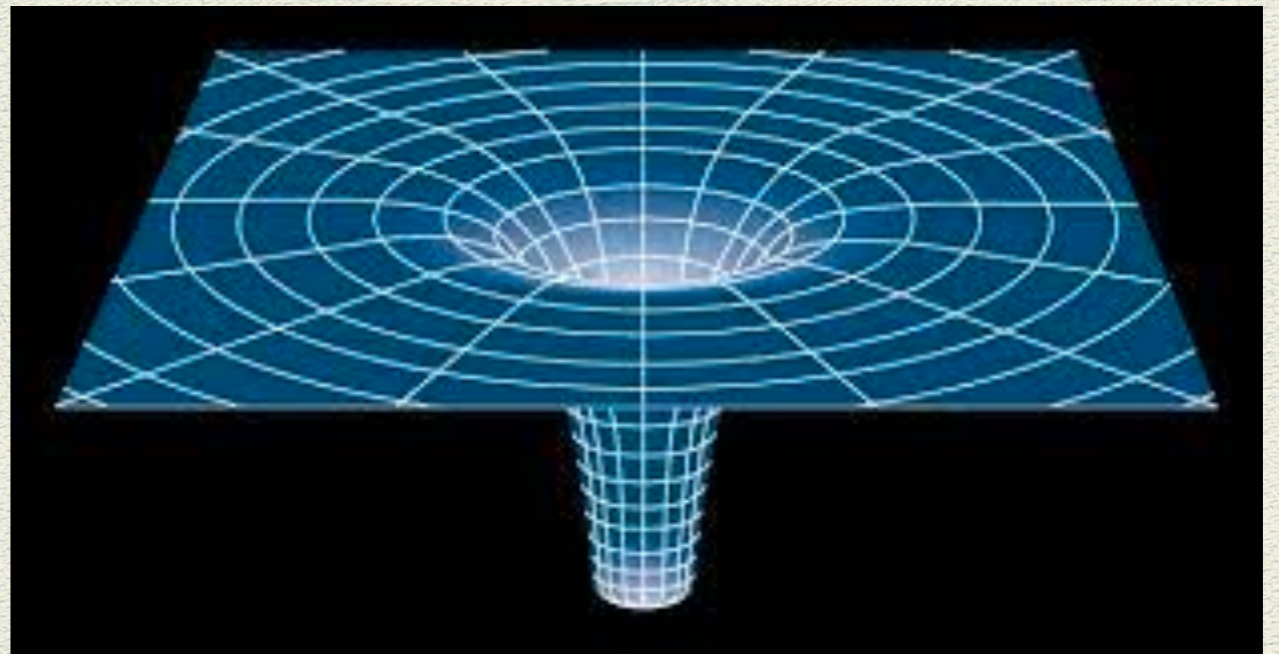
$$S \leq \frac{2\pi k R E}{\hbar c}$$

$$S \leq \frac{2\pi k R_s M c^2}{\hbar c}$$

$$R_s = \frac{2GM}{c^2}$$

$$S \leq \frac{\pi k R_s^2}{\frac{G\hbar}{c^3}} \sim \frac{k A}{4 l_p^2}$$

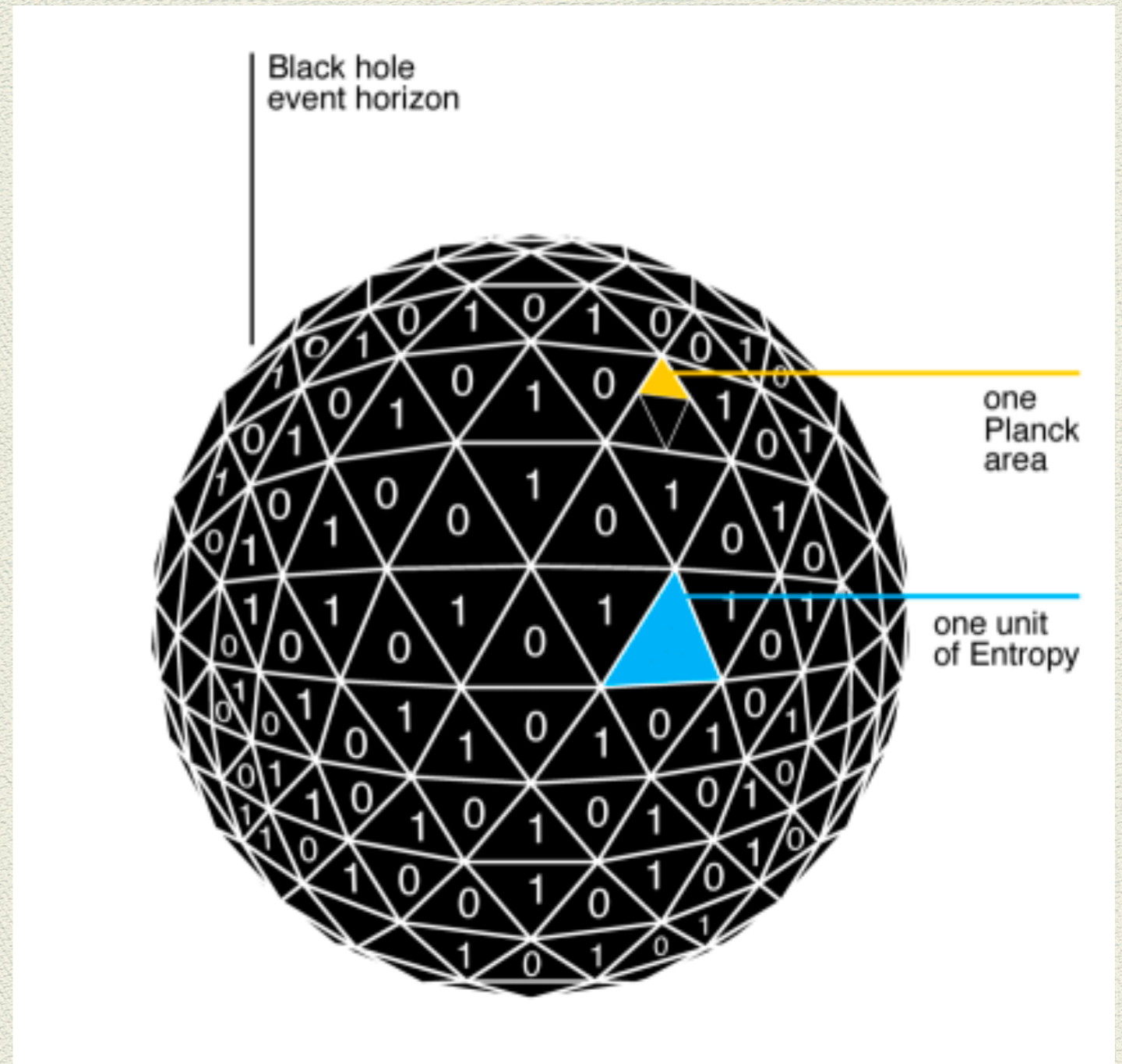
$$I \leq \frac{A}{4 l_p^2}$$



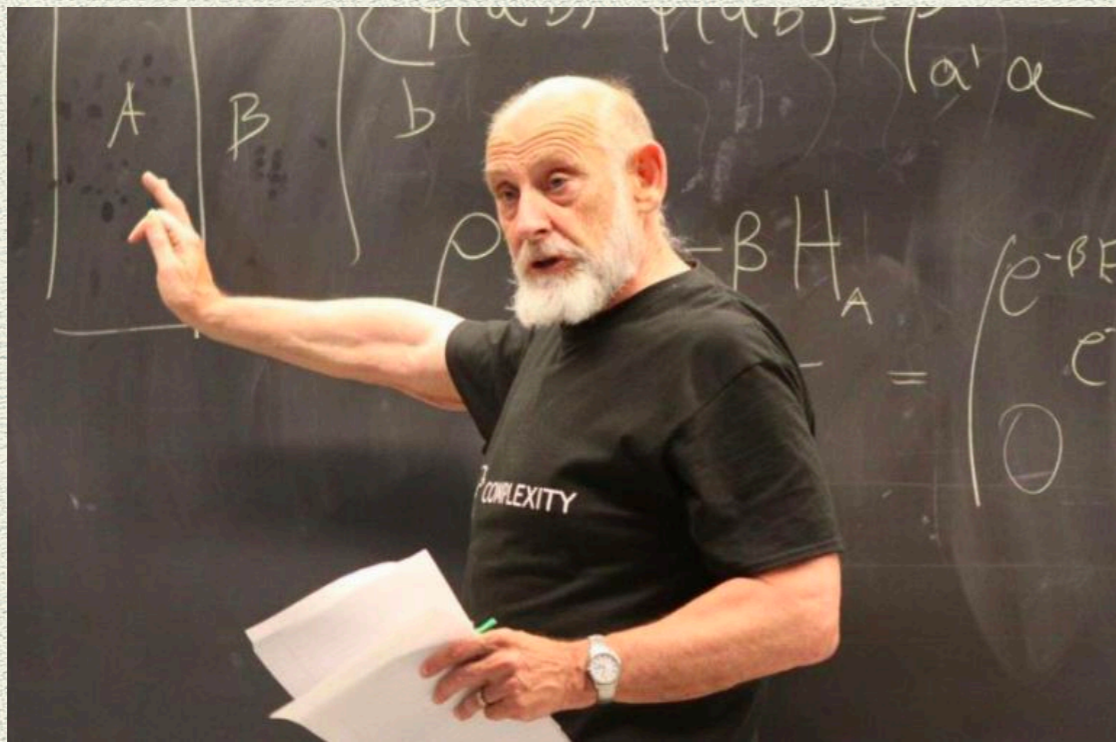
Conjecture: Information is carved on the surface of the black hole

$$S \leq \frac{\pi k R_s^2}{\frac{G\hbar}{c^3}} \sim \frac{k A}{4 l_p^2}$$

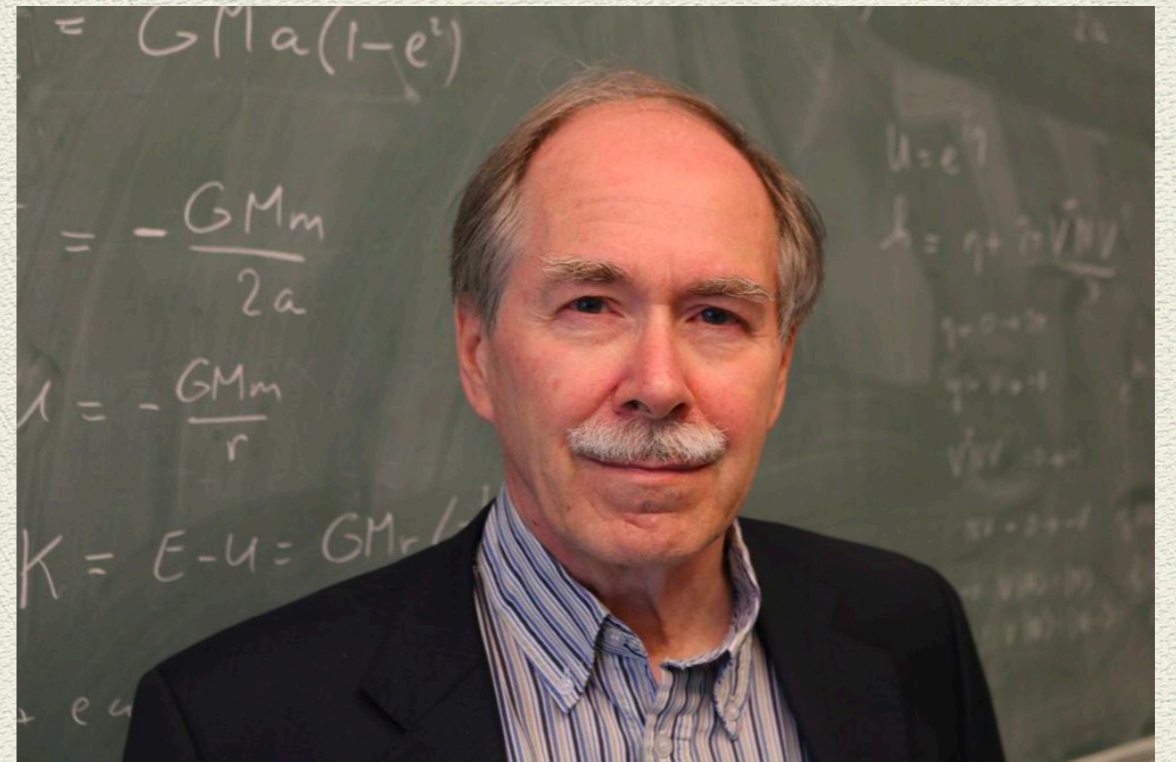
$$I \leq \frac{A}{4 l_p^2}$$



Holography



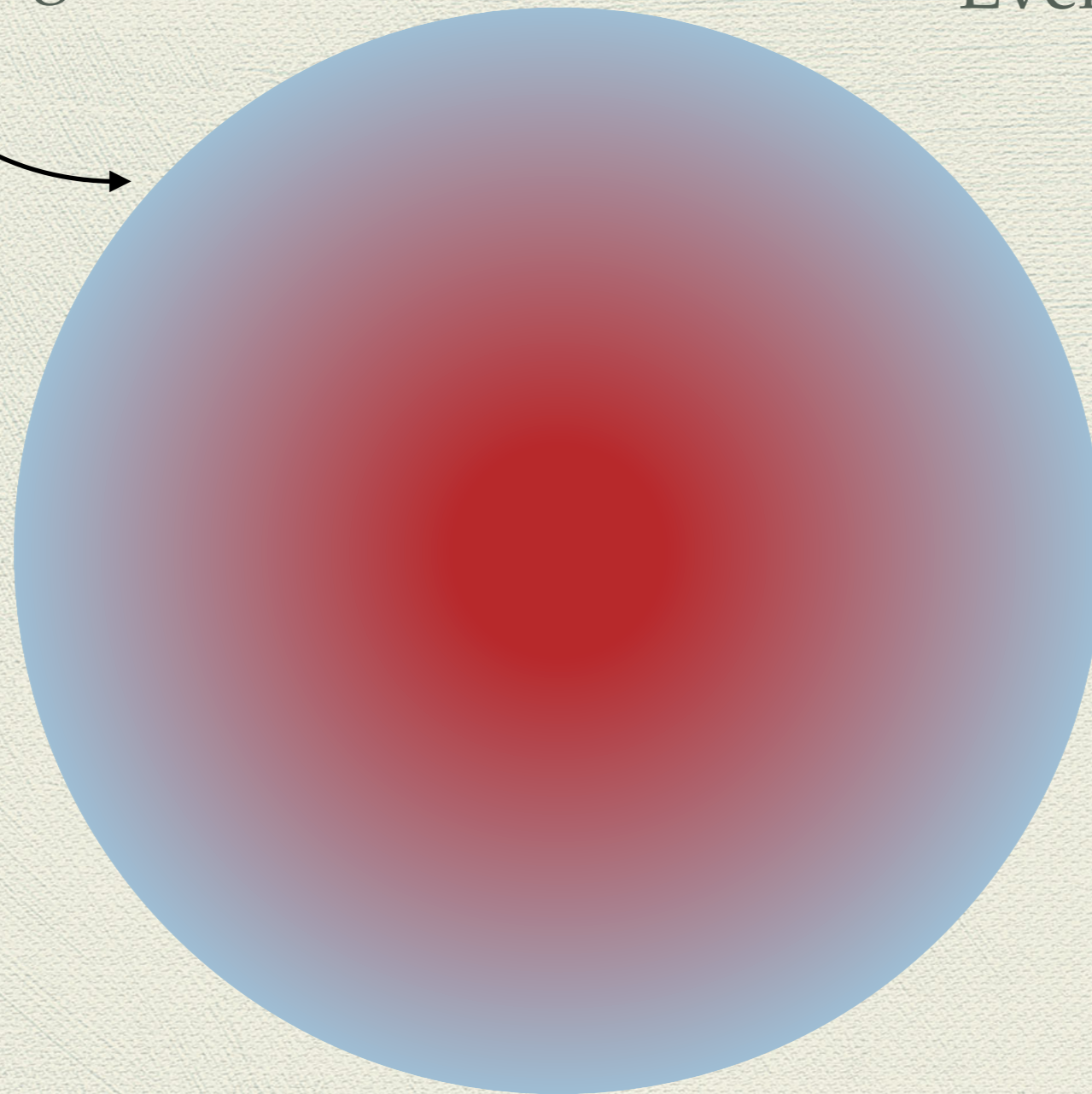
Susskind



't Hooft

The 2D hologram

Event Horizon



Holographic Principle

End of part I